

Investigation of One and Two Nucleon Separation Energies for Checking the Nuclear Stability in the region atomic number between 20 and 35

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Physics

(Nuclear Physics)

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Declaration

I hereby declare that this MSc thesis is my original work and has not been presented for a degree in any other university, and that all sources of material used for the thesis have been duly acknowledged.

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Abstract

Study and measuring nuclear binding energy are most active areas of nuclear structure physics. In this work, Bethe-Weisacker formula has been employed to study binding and nucleon separation energies of different isotopes and isotones for checking the nuclear stability in the region between atomic number 20 and 35. In data calculations, analytical and computational methods have been employed. The calculated binding energy by using Sci-lab computer soft-ware and graphs that were plotted by using xmgrace agree quite well with experimental data and were compared with values given in previous work for the purpose of validity. This work has determined, the relations between one nucleon and two nucleon separation energies with the nucleon number that were plotted Single and double nucleon separation energies in all possible manner and tried to discuss nuclear structure properties such magic nuclei, proton or neutron drip line, nuclear stability and so on. It is clear stated that even-Z and even-N nuclei, being most stable, are most abundant. The results show that stability of nuclei depends on the separation energy is high or not. Moreover, this work has incorporated to indicate many nuclides and transitions of a nuclei having high separation energy are highly stable and abundant.

Key words: Binding Energy, nucleon separation energy, Liquid Drop Model, Shell Model, magic number and nuclear stability.

Introduction

1.1 Back ground of study

Nuclear structural calculation far from the region of stability reveals new ideas which are not usually observed in the stability line. These studies provide information about the type of separation energy and the deformation exhibited by the nuclei. Ground state proton emission is an identification that the drip line has reached. To know about the two proton decay process, their separation energies need to be calculated. The special quality of proton rich nuclei is the di-proton emission. Due to pairing, a nucleus with an even number of protons is tightly bound than odd number of proton nucleus [1]. Hence the existence of two proton emission is sensitive to the two proton separation energies. More number of nuclei is found to undergo one proton emission either from the ground state or from an isomeric state or both. When the emitters are found to be deformed, it gives a check for the nuclear structure models at the drip line [2].

Systematic studies related to nucleon separation energies from the masses of nuclei provide evidence for shell closures. It is important to look for new shell closures or the disappearance of existing shell closures from the separation energy calculation. The origin of the unusual stability of nuclei with nucleon numbers 2, 8, 20, 28, 50, 82 and 126, commonly called to as magic numbers, is explained to be due to nuclear shell structure. At present there is a proliferation of new magic or rather quasi-magic numbers [3, 4]. At the same time some magic numbers are demoted and seem to lose their magicity.

In the simple shell model these are due to shell or sub-shell closures. Shell closure may be demonstrated by a large drop in separation energies. Such phenomena can be simply explained by the simple shell model. The single- and two-nucleon separation energies are fundamental properties of the atomic nucleus. It is a challenge for nuclear many-body theories to derive the shell model out of complex calculations. Systematic of proton and neutron separation energies can be powerful tools to study the nuclear structure at and even beyond the drip lines. It can be used to predict masses and separation energies of nuclei beyond the neutron and proton drip lines.

The shells for protons and for neutrons are independent of each other. Therefore, "magic nuclei" exist in which one nucleon type proton or neutron is at a magic number, and "doubly magic nuclei", where both are. Due to some variations in orbital filling, the upper magic numbers are 126 and, speculatively, 184 for neutrons but only 114 for protons, playing a role in the search for the so-called island of stability. Some semi magic numbers have been found, notably Z = 40 giving nuclear shell filling for the various elements; 16 may also be a magic number [5].

The binding energy is usually plotted as binding energy per nucleon, B/A. The dependence of B/A on A (and Z) is captured by the semi-empirical mass formula. This formula is based on first principle considerations (a model for the nuclear force) and on experimental evidence to find the exact parameters defining it. In this model, the socalled liquid-drop model, all nucleons are uniformly distributed inside a nucleus and are bound together by the nuclear force while the Coulomb interaction causes repulsion among protons. Characteristics of the nuclear force (its short range) and of the Coulomb interaction explain part of the semi-empirical mass formula. However, other (smaller) corrections have been introduced to take into account variations in the binding energy that emerge because of its quantum-mechanical nature (and that give rise to the nuclear shell model).

Stability is all based on the nucleus tending towards the lowest energy state. Stable atoms have low energy states. Unstable atoms will try and become stable by getting to a lower energy state. They will typically do this by emitting some form of radioactivity and change in the process. The shell structure has been believed to be basically common not only among stable nuclei but also between stable and exotic (unstable) nuclei. The ionization energies vary with respect to the numbers of electrons of the atoms except at the shell edges, whereas the separation energies vary in a complicated way with the numbers of protons and neutrons. We have to understand the behavior of the dependence of the nuclear stability on separation energy for the third closed shell, those are atomic number 20-28 isotopes. By applying this knowledge we need a theory which gives the separation energies of nuclei as a function of the numbers of protons and neutrons for the higher mass region, whose sole behavior is not exactly known, because we must take into account the change of the nuclear structure when a nucleon is removed. This study will discuss such variation of separation energy relating with nucleon number of the isotopes and also investigate the relation with nuclear stability if one and two nucleon removed from the nucleus.

1.2 statement of the problem

Nucleon separation energy is the energy needed to remove nucleon (Proton, neutron) from a nucleus. For a given proton number, the neutron separation energy is larger for some nuclei than the other depending on whether the neutron numbers are odd or even [1]. Similarly for the proton separation energy with constant number of neutrons the energy needed to separate one proton or two protons is not the same; it rather depends on the number of neutrons in the nucleus [4].

Even-even nuclei occur most frequently than odd-odd nuclei in the table of stable nuclides available in nature. If stable nuclei were formed by a process in which increased binding energy produce increased abundance, we could deduce that those nuclei with higher value of binding energy are the most stable that is we can connect abundance with stability. This may has some connection with systematic of separation energies of the nucleon [6]. In this thesis therefore we can justify stability of a nucleus as evidenced by nucleon separation energies for a range of isotopes with proton number between 20 and 35.

The research leading questions that were answered are:

- 1. What relations are there between single nucleon and two nucleon separation energies and the nucleon number?
- 2. What are the factors that affect nucleon separation energy of nuclei for a given

proton/neutron number?

3. What conclusion can be drawn to predict nuclear stability from nuclear separation energies?

1.3 Objectives of the study

1.3.1 General Objective

The main objective of this study is to calculate one nucleon and two nucleon separation energies and investigate the relation between the separation energies and the nuclear stability of medium mass (i.e $20 \le Z \le 35$).

1.3.2 specific objectives

The specific objectives of this study are :

- 1. To explain the relations between one nucleon and two nucleon separation energies with the nucleon number.
- 2. Discuss the factors that affect nucleon separation energy of nuclei for a given nucleon number.
- 3. To clarify the relation of nucleon separation energies and stability.

1.4 Significance of the Study

Obtaining theoretical conclusion on the application of nucleon separation energies to check for the nucleon closed shells and nuclear stability for the given isotopes which lies below the second nucleon closed shell is the main relevance of this research. In addition it can be used as a reference to use in similar researches.

1.5 Limitation of the Study

The research study was not free from limitation. Lack of advanced laboratory made to limit the study only theoretical consideration. similarly Due to time constraint the study were limited to calculation of nucleon separation energies for the isotopes whose structure lies in the second closed shell region, other shell closures were not be checked. The other limitations that might bring some impact on the result of the study are lack of recurrence material and finance and also lack of sufficiently fast internet connection in the local area where the research thesis was developed.

Review of Literature

2.1 Models of Nuclear Structure

A goal of nuclear physics is to account for the properties of nuclei in terms of mathematical models of their structure and internal motion. Two important nuclear models are the Liquid Drop Model and the Shell Model (developed by Maria Goeppert-Mayer and Hans Jensen) [5], which emphasizes the orbits of individual nucleons in the nucleus[3]. The Liquid Drop Model treats the nucleus as a liquid. Nuclear properties, such as the binding energy, are described in different parameters that are usually associated with a liquid. This model has been successful in describing how a nucleus can deform and undergo fission.

The Nuclear Shell Model is similar to the atomic model where electrons arrange themselves into shells around the nucleus. The least tightly-bound electrons (in the incomplete shells) are known as valence electrons because they can participate in exchange or rearrangement, that is, chemical reactions [3]. The shell structure is due to the quantum nature of electrons and the fact that nucleons are fermionsparticles of half-integer spin. Consequently the fermions in a bound system will gradually fill up the available states: the lowest one first, then the next higher unoccupied state, and so on up to the valence shell [4].

2.2 Liquid drop model

One of the first nuclear models, proposed in 1935 by Bohr, is based on the short range of nuclear forces, together with the additivity of volumes and of binding energies. It is called the liquid-drop model. Nucleons interact strongly with their nearest neighbors, just as molecules do in a drop of water. Therefore, one can attempt to describe their classical properties by the corresponding quantities, i.e. the radius, the density, the surface tension and the volume energy.

An excellent parameterization of the binding energies of nuclei in their ground state was proposed by Bethe and Weizsacker [7]. This formula relies on the liquid-drop analogy but also incorporates different quantum ingredients. One is an asymmetry energy which tends to favor equal numbers of protons and neutrons. The other is a pairing energy which favors configurations where two identical fermions or nucleon are paired.

- The nucleons in a nucleus behave like molecules in the liquid drop.
- The emission of nuclear radiations (n, p, d and so on) from nucleus is analogous to the emission of the molecules from the liquid drop during evaporation.
- The constant B.E. per nucleon is analogous to the constant latent heat of vaporisation of the liquid.

The average behaviour of the nuclear binding energy can be understood with the model of a charged liquid drop. In this model, the aggregate of nucleons has the same properties of a liquid drop, such as surface tension, cohesion, and deformation. There is a dominant attractive binding energy term proportional to the number of nucleons A. From this must be subtracted a surface-energy term proportional to surface area and a coulombic repulsion energy proportional to the square of the number of protons and inversely proportional to the nuclear radius. Furthermore, there is a symmetry-energy term of quantum-mechanical origin favouring equal numbers of protons and neutrons. Finally, there is a pairing term that gives slight extra binding to nuclei with even numbers of neutrons or protons.

2.3 Nuclear Shell model

Atomic theory based on the shell model has provided remarkable classification of the complicated details of atomic structure. Nuclear physicists therefore attempted to use

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a similar theory to attack the problems of nuclear structure in the hope of similar success in classifying the properties of nuclei. In the atomic shell model we fill the shells with electrons in order of increasing energy consistent with the requirement of the Pauli principle. when we do so, we obtain an inert core of filled shells and some number of valance electrons; the model then assumes that atomic properties are determined primarily by the valance electrons. in particular we see regular and smooth variations of atomic properties within a sub-shell, but rather sudden and dramatic changes in the properties when we fill one sub-shell and enter the next[8].

Nuclei near major shell closures may be described microscopically by the shell model. The properties of these nuclei have been predicted in good agreement with experiment considering an extreme single-particle shell model. According to this model, the properties of the nucleus are dictated by the behavior of a single unpaired nucleon.

These models are necessary for the extrapolation of single-particle properties of nuclei far from stability[5]. Doubly-magic nuclei those that have a magic number for both protons and neutrons are crucial for the understanding of nuclear structure. The closed-shell property of the doubly-magic nuclei provides a good zeroth-order wave function which can be systematically improved upon by using perturbation theory. Starting with a zero-particle zero-hole (0p-0h) closed shell, the structure of the closed shells themselves can be systematically improved by the mixing of 2p-2h and higher excitation.

- The binding energies of magic-number nuclei is much larger than in the neighboring nuclei. Thus larger energy is required to separate a single nucleon from magic nuclei.
- The number of stable nuclei with magic values of proton number, Z or neutron number, N is much larger than the corresponding number in neighboring nuclei.
- Naturally occurring isotopes with magic Z or N have greater relative abundances.
- The first excited states in nuclei with magic numbers of neutrons or protons lie at higher energies than the same states in neighboring nuclei.

There is thus a correction term in the Semi-emprical mass formula which tries to take into account the symmetry in protons and neutrons. Symmetry and pairing term correction can only be explained by a more complex model of the nucleus, the shell model, together with the quantum-mechanical exclusion principle.

2.4 Estimating Binding energy using Bete-Von Weisacker formula

2.4.1 Binding energy of the nuclei

The mass of an atomic nucleus is less than the sum of the individual masses of the free constituent protons and neutrons, according to Einstein's equation $E = mc^2$ [9]. This 'missing mass' is known as the mass defect Δm , and represents the energy that was released when the nucleus was formed. The binding energy is equal to the amount of energy released in forming the nucleus, and is therefore given by

$$B.E = \Delta mc^2 \tag{2.1}$$

Binding energies are crucial to understand why a nucleus exists, and they can be used to explain why only specific combinations of protons and neutrons are found in nature or in experimental nuclear physics facilities.

The mass of a stable nucleus in its ground state is always less than the masses of the protons and neutrons composing the nucleus. We write the energy of the nucleus in the ground state [10, 11]:

$$E(A,Z) = M(A,Z) - ZMp - (A-Z)Mnc^{2}$$
(2.2)

where E(A,Z) is the mass of the nucleus and Mp and Mn are the mass of the proton and neutron respectively. The quantity E(A,Z) taken with the opposite sign is called the binding energy. Clearly, the binding energy is the work that must be expended to break up the nucleus into its constituent particles.

The binding energy of an isotope of element Z with N neutrons is defined by the difference:

$$B.E = [Nm_n + Zm_p - M(N, Z)]c^2$$
(2.3)



Figure 2.1: Average binding energy per nucleon (MeV) versus mass number, A

where $m_n c^2 = 939.565$ MeV and $m_p c^2 = 938.272$ MeV represent the rest mass energies of the neutron and the proton, and M(N,Z) is the rest mass of the nucleus itself. The binding energy per nucleon is characteristic of the stability of the nucleus. Figure 2.1 shows the dependence of the mean binding energy per nucleon on the mass number, A for different nuclei. The binding energy per nucleon first increases rapidly with increasing A, attaining a value of 8 MeV by A = 16, then increases very slowly to a value of 8.8 MeV at A 60, and then decreases very slowly, taking the value 7.4 MeV for the heaviest nuclei [8].

The most characteristic feature of this dependence is the fact that the mean binding energy per nucleon is approximately constant (8 MeV) over almost the whole range of variation of A, with the exception of the region of very light nuclei. Consequently, the total nuclear binding energy, like the nuclear volume, is proportional to the number of nucleons in the nucleus. Small deviations from this proportionality are connected with surface effects, the Coulomb repulsion between the protons, the difference between the numbers of protons and neutrons, and the effect of the parity of the numbers of protons and neutrons. The fact that the mean binding energy per nucleon, like the volume per nucleon, is independent of the number of nucleons in the nucleus can be explained by assuming that the nuclear forces between the nucleons possess the property of saturation, that is, each nucleon in the nucleus can interact only with a small number of nearest nucleons. As binding energy per nucleon increases the nuclear stability of light nuclei highly increase.

The saturation of the nuclear forces points to an analogy between the properties of the nuclear substance and those of an ordinary liquid. On the basis of this analogy, a liquid-drop model of the nucleus is introduced, according to which the nucleus can be regarded as a drop of nuclear liquid. The liquid-drop model of the nucleus makes it possible to explain the dependence of the nuclear binding energy on the mass number A and the charge Z of the nucleus.

2.4.2 Weisacker formula for Binding Energy

The analogy between nucleus and liquid drop has been used to set up a Weisacker (semi-empirical) formula for mass (or binding energy) of a nucleus in its ground state [10]. The formula has been obtained by considering different factors of the nucleus binding. The binding energy B of a nucleus is given by the sum of five terms as

$$B = B_1 + B_2 + B_3 + B_4 + B_5 \tag{2.4}$$

Which are explained as under different terms:

Volume Energy Term (B_1): The binding energy is a measure of the interaction among nucleons. Since nucleons are closely packed in the nucleus and the nuclear force has a very short range, each nucleon ends up interacting only with a few neighbors. This means that independently of the total number of nucleons, each one of them contribute in the same way. This is same as the binding energy of the drop B. So

$$B = LMnN \tag{2.5}$$

where N is the number of molecules in the drop. Equation (2.5) can also be written as

$$\frac{B}{N} = LMn = constant \tag{2.6}$$

This means that B/N is independent of the number of molecules present in the liquid drop. As we know that in the liquid drop, a molecule interacts only with its nearest

neighbours and number of neighbors is independent of the size of the drop. The neutrons and protons are held together in nuclei by short range attractive forces.

Since the volume of the nucleus is proportional to A, hence this term is regarded as a volume binding energy and in analogy above equation is given by:

$$B_1 = a_v A \tag{2.7}$$

where a_v is a proportionality constant and subscript v is for volume.

The surface term (B_2) : is a correction to the volume term to take into account that the nucleons at the surface of the nucleus do not have the same level of interactions as nucleons in the interior of the nucleus. In the above volume term discussion, we have assumed that all the molecules are surrounded by its neighbors, while in actual practice the molecules at the surface do not have any neighbors on all the sides. So these molecules are not as tightly bound as the molecules in the interior. Extending this argument to the nuclear case, some nucleons are nearer to the surface, and so they interact with fewer nucleons [10].

Thus, the binding energy is reduced by an amount proportional to the surface area of the nucleus of radius r as the nucleons on the surface are less tightly bound than those in the interior. This term is proportional to the surface area of the nucleus of radius $R = r_0 A^{\frac{1}{3}}$. Therefore,

$$B_2 \propto -4\pi r^2 \tag{2.8}$$

$$B_2 \propto -4\pi r_0^2 A^{\frac{2}{3}} \tag{2.9}$$

Which is usually expressed as:

$$B_2 = -a_s A^{\frac{2}{3}} \tag{2.10}$$

Where negative sign is for decrease in energy and a_s is constant.

Coulomb Energy Term (B_3) : The Coulomb term represents the energy incorporated in the nucleus as a result of the positive charge present in the nucleus. The only longrange force in the nucleus is the Coulomb repulsion between protons [10]. The total work done in assembling a nucleus consisting of *Z* protons is given by:

$$W = \frac{\frac{3}{5}Z^2 e^2}{4\pi\epsilon_0 r}$$
(2.11)

Where r is the radius of the nucleus. For a single-proton nucleus

$$w = \frac{\frac{3}{5}e^2}{4\pi\epsilon_0 r}$$
(2.12)

For a nucleus having Z protons

$$w' = \frac{\frac{3}{5}Ze^2}{4\pi\epsilon_0 r}$$
(2.13)

For a single-proton nucleus no work is done against Coulomb repulsion in assembling the nucleus. Thus, the true Coulomb energy term for a nucleus containing Z protons is the difference between eq. (2.24) and (2.26).

$$B_3 = -\left[\frac{\frac{3}{5}Z^2e^2}{4\pi\epsilon_0 r} - \frac{Z\frac{3}{5}e^2}{4\pi\epsilon_0 r}\right]$$
(2.14)

That is

$$B_3 = -\frac{3}{5} \frac{Z(Z-1)e^2}{4\pi\epsilon_0 r}$$
(2.15)

The negative sign indicates the repulsive term. As $R = r_0 A^{\frac{1}{3}}$, then

$$B_3 = -a_c \frac{Z(Z-1)}{A^{\frac{1}{3}}} \tag{2.16}$$

where a_c is constant.

Asymmetry Energy Term (B_4): The asymmetry term reflects the stability of nuclei with the proton and neutron numbers being approximately equal. This is a term, which depends on the neutron excess (N-Z) in the nucleus and it decreases with the increasing nuclear binding energy. For very few nuclei of low Z, N-Z = 0 and are more stable compared to their neighbors, i.e. their binding energies are maximum. The reduction in binding energy for higher A nuclei is directly proportional to $(N - Z)^2$ or square of excess of neutrons and is inversely proportional to mass number. So, we can write

$$B_4 \propto \frac{(N-Z)^2}{A} \tag{2.17}$$

Z	N	Number of stable nuclide
Even	even	165
Even	odd	55
Odd	even	50
Odd	odd	5

Table 2.1: Four group of stable nuclei

$$B_4 = -a_a \frac{(A - 2Z)^2}{A}$$
(2.18)

As A = N + Z and a_a is constant.

Pairing Energy Term (B_5): So far we have all the terms in the binding energy have smooth variation with respect to N or Z or A. This fact did not appear in the liquid drop model, which does not consider intrinsic spin of the nucleons and the shell effects. It is interesting to classify all the stable nuclei into four groups, first having even-even , even-odd N, odd-even and odd Z-N.

From Table 2.1, it is clear that even-Z and even-N nuclei, being most stable, are most abundant. Accordingly, odd-Z and odd-N nuclei are least abundant and hence least stable. The remaining nuclei have intermediate stability. Therefore, the binding energy also depends upon whether the number of protons and neutrons are odd or even. This pairing effect was incorporated by putting:

$$B_5 = a_p A^{-\frac{1}{2}} \tag{2.19}$$

Substituting the values of B_1 , B_2 , B_3 , B_4 and B_5 from above term Equations, then the Weisacker formula for Binding Energy is:

$$B = a_v A - a_s A^{\frac{2}{3}} - a_c \frac{Z(Z-1)}{A^{\frac{1}{3}}} - a_a \frac{(A-2Z)^2}{A} + a_p A^{-\frac{1}{2}}$$
(2.20)

The various constants found are:

 $a_a=23.0 \text{MeV}$

a_p=34MeV, 0MeV, -34MeV for even-even, even-odd and odd-odd nuclei respectively.

2.5 Nuclear stability

For stable nuclides having atomic number Z < 20, N=Z, for Z > 20 the number of neutrons has to be greater than Z for stability of the nucleus. This is because for stable nuclei having large values of Z. The Coulomb force of repulsion between the protons becomes very large. In order to compensate the large repulsion force there has to be greater number of neutron [11]. Nature seeks the lowest energy state. In the lowest energy state, things are most stable...less likely to change. One way to view this is that energy makes things happen. If an atom is at its lowest energy state, it has no energy to spare to make a change occur. The following information that talks about stability is all based on the nucleus tending towards the lowest energy state. Stable atoms have low energy states. Unstable atoms will try and become stable by getting to a lower energy state. They will typically do this by emitting some form of radioactivity and change in the process.

Heisenberg and Majorana proposed in 1933 a theory of nuclear forces based on the proton neutrons constitution of the nucleus and a suitable combination of the liquid drop and shell models, which was able to explain several of the experimentally observed facts concerning the stability of nuclei satisfactorily though not completely. Majorana also explain the electrostatic repulsive forces between the protons in the nucleus.

However, because of the saturation character of the intra-nuclear forces, the Coulomb repulsion between the protons becomes important for heavy nuclei. The Coulomb forces show no saturation. Hence the total energy of the Coulomb interaction need not be proportional to the mass number A. The binding energy per nucleon will there-fore decrease, on account of the electrostatic force; with increasing mass number as is actually the case with heavier nuclei, this work in the opposite direction from the surface tension effect.

It is fount that nuclear forces holding the nucleons together inside the nucleus, which

are short range, basically very strong about 10^{38} times as strong gravitational forces, charge independent (i.e, n-p= n-n =P-P), charge symmetric, spin dependent and non-central forces. These forces of attraction are much larger than the electrostatic force of repulsion between the protons, thus giving stability to the nucleus.

2.6 Nucleon separation Energy

Separation energy is the energy needed to remove one nucleon (or other specified particle or particles) from an atomic nucleus. The separation energy is different for each nuclide and particle to be removed. Values are stated as "neutron separation energy", "two-neutron separation energy", "proton separation energy", "deuteron separation energy", "alpha separation energy", and so on [12]. Difference of binding energy of two neighboring isotopes yield the separation energy of one neutron. The smallest energy required to remove a nucleon from the nucleus is the separation energy (S). For medium heavy nuclei the separation energy for a neutrons n is approximately equal to the separation energy for a proton S_p , but for lighter nuclei both S_n and S_p show considerable fluctuations.

By contrast, nuclear binding energy is the energy needed to completely disassemble a nucleus, or the energy released when a nucleus is assembled from nucleons. It is the sum of multiple separation energies, which should add to the same total regardless of the order of assembly or disassembly.

Nucleon separation energy plays an important role in predicting new shell closures in the proton and neutron drip line nuclei. The one and two nucleon separation energies are fundamental properties of the atomic nucleus. The systematic study of proton and neutron separation energies is essential to investigate nuclear structure toward drip lines [12, 13]. In literature it is understood that the energy spend in removing two fermions from a system of identical fermions shows system stability. If the pairing dominates in fermion-fermion interaction, then energy required to separate two fermions for even number of particles will be much higher than odd number. These characteristics can be observed from the study of two neutron separation energy S_{2n} . It is known

that in neutron-rich nuclei, odd magic numbers disappear and new ones appear.

The drip line is reached when the separation energy reaches zero; hence, for example one can talk about the one-neutron drip line when $S_n = 0$ and the two-neutron drip line when $S_{2n} = 0$. Very weakly bound, or unbound, nuclei that lie in the immediate vicinity of drip lines are referred to as threshold systems.

One neutrons separation energy is the required energy to remove One neutrons from a nucleus with Z protons and N neutrons.

The proton- and the neutron separation energy of a nuclide with numbers N and Z are given by:

$$S_p(N,Z) = B(N,Z) - B(N,Z-1)$$
(2.21)

$$S_n(N,Z) = B(N,Z) - B(N-1,Z)$$
(2.22)

The B(N, Z) is the binding energy of the nuclide related to its mass M(N, Z):

$$M(N,Z) = ZM_H + Nm_n - B(N,Z)$$
(2.23)

Where M_H and m_n are masses of the hydrogen atom and the neutron, respectively. When we move along the line of isotopes with the given atomic number Z, starting from stability towards nucleon-deficient nuclides, the proton/neutron separation energy S_p decreases and at certain location it becomes negative. The proton drip-line is defined as the border between the last proton-bound isotope and the first one with the negative value of the S_p .

The drip lines as defined above are very useful in identifying and discussing limits of stability, but to some extend they are arbitrary and they do not provide the unambiguous demarcation of nuclear stability. This can be seen by inspecting the twonucleon separation energies [14]:

$$S_{2P}(N,Z) = B(N,Z) - B(N,Z-2)$$
(2.24)

$$S_{2n}(N,Z) = B(N,Z) - B(N-2,Z)$$
(2.25)

The particle stability of a nuclide is determined by its separation energy, i.e., the energy required to remove from it a single nucleon or a pair of like nucleons. If the separation energy is positive, the nucleus is bound to nucleon decay; if the separation energy is negative, the nucleus is particle-unstable.

Materials and Method

3.1 Materials

The following list of materials and Soft-wares were used during the work: Computer, printer, Sci-lab computer soft ware, Published Articles and Journals and Books, Flush disc and Stationary materials.

3.2 Method

3.2.1 Analytic Method

The resulting output of level the separation energies were plotted as a function of neutron number and proton number to see the pattern and some conclusion were drawn to predict the nuclear stability from the data (that displayed in table).

3.2.2 computational method

Using liquid drop model the weiszacker formula derived equations a Sci-Lab software were used to calculate Binding energy and then one nucleon and two nucleons separation energies. Using the calculated data, the nucleon separation energies for those isotopes and isotones (stable and unstable) [15,16] which lies under the second closed shell in their structure were calculated and the result were listed in a table and saved in a computer.

4

Results and Discusion

4.1 Results and Discussion

Under this section the one and two Nucleon separation energies for checking the Nuclear stability in the region between atomic number 20 and 35 were discussed. Firstly binding energy(BE) were calculated by using Bethe-Weisacker mass formula (equation 2.20). After these calculation of Binding energy were finished, we were able to use these binding energies to calculate different single and double nucleon separation energy values for single proton(S_p), single neutron(S_n), two protons(S_{2p}), and two neutrons(S_{2n}) by using equation 2.21, 2.22, 2.24, and 2.25 respectively, for different isotones and isotopes of atomic number between 20 and 35 (i.e Ca, Sc, Ti, V, Cr, Mn, Ir, Co, Ni, Cu, Zn, Ga, Ge, As, Se, and Br). The separation energies calculated for different proton numbers, Z for fixed values of neutron number, N and different neutron numbers for various fixed Z values. All data of Binding energy and separation energy calculated were presented in table 4.1.

4.2 Single Nucleon Separation Energy in the region $20 \le Z \le 35$

Under this section Single proton and Single neutron separation as a function of nucleons were discussed depends on the data from the calculation of Single nucleon separation energies in the region of $20 \le Z \le 35$ which were displayed in the table 5.1.

4.2.1 Single proton Separation Energy for fixed proton number

As we can see in Figure 4.1, Single proton separation energy increases as the neutron number of the given isotope increase. We can understand here that, additional neutrons requires to assure nuclear stability this is because of the asymmetry term effect. For instance Scandium isotopes black colored (Z=21) curve, the single proton separation energy of ⁴⁰Sc (S_p = 0.4 MeV) is about 1/50th of ⁶¹Sc (S_p = 21.72 MeV), in Titanium isotopes red colored (Z=22) curve, ³⁹Ti have (S_p = 1.04 MeV) but ⁶²Ti have (S_p = 23.21 MeV), which is much much greater than separation energy of ³⁹Ti. And also ⁹⁶Br have a 14.68 MeV single proton separation energy which is 60 times greater than single proton separation energy of ⁶⁹Br is (S_p = 0.24 MeV). And this increasing pattern in the given Figure 4.1 is true for all isotopes of the nuclei in the region of atomic number between 20 and 35.

When we move along the line of isotopes with the given atomic number Z, starting from stability towards neutron-deficient nuclides, the proton separation energy S_p decreases and at certain location it becomes negative. This point is proton drip-line that is the border between the last proton-bound isotope and the first one with the negative value of the S_p . In this region there are isotopes having negative separation energy. These negative separation energy indicates that nucleon will not bind to the rest of the nucleus. Such a configuration is also called particle unstable, because the nucleus will decay by proton emission. Therefore the location of the drip line is determined by the separation energy crossing zero. These isotopes are unstable (that is, radioactive) nuclei. Thus, the one proton drip line is reached when $Sp \leq 0$, which means the proton-drip line lies close to the valley of stability. (For instance as shown in Figure 4.1 the ³⁸Sc, ⁴⁵Mn, ⁴⁶Mn, ⁴⁸Co, ⁴⁹Co, ⁴⁹Ni, ⁵⁰Ni, and soon have negative value of one proton separation energy).

The isotopes of the atomic number between 20 and 35, single proton separation energy increases as a function of neutron number increase, especially in different isotopes at N= 20, 28, and 50 it suddenly increases as it approaches the magic nuclei. The sharp discontinuities in separation energies correspond to filling of shells in the single proton separation energies of sequences of isotopes. Which means hardly affects the values of S_p when N = 20, 28, 50. This is a consequence of Neutron numbers being a magic



Figure 4.1: Single proton separation energy as a function of N for different Z values.

number.

4.2.2 Single Neutron Separation Energy for fixed proton number

Under this section the discussion is based on Figure 4.2 and 4.3, One Neutron Separation Energy as a function of neutron for constant proton number we can see that separation energy is noticeably higher if the number of neutrons is even. If a neutron is removed from a nucleus with an even number of neutrons, a pair must be broken up that requires additional energy. A single neutron separation energy not follow the same pattern with single proton separation energy discussed above, rather it fluctuate depending on the evenness and oddness of the nucleon numbers of the nuclei as described pairing term in weisacker formula. Nuclear pairing generally tends to stabilize even-even species than their odd-odd neighbors. Because of this in the Figure 4.2 the maximum (up) peaks have even-even nuclei while minimum (down) peaks have odd neutron number. Similarly Figure 4.3 the up peaks have even neutron while down peaks have odd neutron number. Due to this stabilization, the one-nucleon drip lines are reached earlier in the nuclear landscape than the two-nucleon drip lines.

This shows that in most cases the nuclei of even nucleon number is more stable than that of odd nucleon number. And also, the single neutron separation is higher to transit from doubly magic nuclei (both proton and neutron number magic) than atomic number magic nuclei. For instance, the single neutron separation energy needed to separate a neutron from ³⁶Ca to transit to ³⁵Ca is more than approximately by 5 MeV of separation energy needed to separate a neutron from ³⁷Ca to transit to ³⁶Ca. Like that of single proton separation energy, in case of single neutron separation energy there are negative separation energies. These negative energies occur when a neutron separated from nuclei of odd nucleon number. In this case isotopes which have a constant number of protons but a varying number of neutrons were considered. For the neutron-rich isotopes of each element, the limit at which any additional neutron will not be bound is called the neutron drip line.

The one-neutron separation energy becomes negative as the neutron drip line is crossed. This means that a nucleus beyond the neutron drip line gains a more stable configuration by emitting one neutron directly. The location of the neutron drip line coincides with the limit of existence of the nucleus, meaning that nuclei beyond the neutron drip line will decay.

Also As shown in Figure 4.2 the neutron separation curve become high at magic number 28 at some extents of points. It shows that separation energies disclose rich nuclear structure information. They indicate very clearly the major shell closures at double magic number (N=28 and Z=28) reflected by discontinuities of one-neutron separation energy as a function of N that is ⁵⁶Ni in Figure 4.2 yellow colored curve. And also ⁴²Ti and ⁵⁰Ti have high one-neutron separation energy because of its N=20 and 28 magic numbers respectively. Nuclear pairing generally tends to stabilize even-even species with respect to their odd-mass or odd-odd neighbors. Because of this in the Figure 4.2 and 4.3 the maximum (up) peaks have even neutron while minimum (down) peaks have odd neutron number number.

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Figure 4.2: Single neutron separation energy as a function of N for different even-Z values.

4.2.3 Single Neutron Separation Energy for fixed Neutron number

As shown in Figure 4.4, single neutron separation energies for isotones corresponding to N = 18 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, and 32 were plotted. One-Neutron separation energies isotonic transition (For instance 38 Ca to 37 Ca, 39 Sc to 38 Sc, 40 Ti to 39 Ti, and 42 Cr to 41 Cr, have a value of 18.06 MeV, 19.35 MeV, 20.56 MeV, and 22.92 MeV respectively) for N=18 black colored curve and other isotones were calculated as a proton numbers varies. As we can see here one neutron separation energy is increases as proton number increase because of the asymmetry energy term effect since its effect is smaller for larger A.

In this section we can found that magic numbers appear and some others disappear in moving from stable to exotic (unstable) due to its neutron-neutron interaction. As shown in Figure 4.4 the one neutron separation become continuously steep up at some extents of points, but it was discontinuity at middle point as the proton number increase, that is when we compare N=20 green colored curves have high separation energy



Figure 4.3: Single neutron separation energy as a function of N for different odd-Z values.

than N=19 red colored curves which indicate very clearly that the magic shell closures at magic number of neutron. The study of Figure 4.4 gives the information that the values of neutron separation energy of the nearest nuclei of magic nuclei are less than that of the magic nuclei.

4.2.4 Single proton Separation Energy for fixed Neutron number

Figure 4.5 were plotted for Single proton separation as a function proton number for fixed neutron number. When we move along the line of isotones, starting from stability towards neutron-deficient nuclides, the proton separation energy S_p decreases and at certain location it becomes negative. For example in Figure 4.5 black colored (N=20)the isotonic transition (i.e ⁴¹Sc to ⁴⁰Ca, ⁴²Ti to ⁴¹Sc, ⁴³V to ⁴²Ti, ⁴⁴Cr to ⁴³V, ⁴⁵Mn to ⁴⁴Cr, ⁴⁶Fe to ⁴⁵Mn, and ⁴⁷Co to ⁴⁶Fe) have one proton separation energy 2.23 MeV, 4.63 MeV, -0.33 MeV, 2.13 MeV, -2.61 MeV, 0.39 MeV, and -1.16 MeV respectively. When we increase protons, asymmetry and Coulomb term reduces the binding energy. Therefore steeper



Figure 4.4: Single neutron separation energy as a function of Z for different N values.

drop of proton separation energy is observed and the drip line is reached much sooner. Increasing of protons makes decrease Binding energy as well as separation energy. This is because of Coulomb repulsion which makes a nucleus containing many protons less favorable for stability.

In addition, according to the pairing term in the Weisacker formula, as the above example indicates, an even number of particles is more stable than odd number. The single neutron separation energy needed to separate one neutron from even nuclei to odd nuclei is greater than neutron separation needed to separate single neutron from odd to even nuclei as shown in Figure 4.5. Because of this the maxima (up) peaks have even proton while minima (down) peaks have odd proton number. The tendency to form proton pairs and neutron pairs is a consequence which arises from this energy term. And also binding energy is high if we have an even-even nucleus, where all the neutrons and all the protons are paired.



Figure 4.5: Single proton separation energy as a function of Z for different N values.

4.3 Two Nucleon Separation Energy in the region $20 \le Z \le 35$

Under this section the discussion for the separation energies of two proton and two neutron have been given depends on the data from the calculation of two nucleon separation energies in the region of $20 \le Z \le 35$ which displayed in the table 5.1 and 5.2.

4.3.1 Two Protons Separation Energy for fixed neutron number

In this work two-protons separation energy as a function of proton number for fixed neutron number (Neutron number =20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, and 32) were calculated. As shown in the Figure 4.6 two proton separation energy decreases as a function of proton number for fixed neutron. Due to increasing of proton number the mass number, A will be large. Because the increasing of the difference between the number of proton and number of neutron the effect of asymmetry energy term become high. Then the two proton separation energy will be decreased.

Similarly the stability of the nuclei will be reduced due to high coulomb's repulsion force in case of adding protons for fixed neutron number. Therefore steeper drop of

two-proton separation energy is observed and the drip line is reached much sooner. As shown on the Figure 4.6, for the neutron-rich isotopes of each element, the limit at which any additional neutron will not be bound is called the neutron drip line. The two-proton separation energy becomes negative as the neutron drip line is crossed. The location of the neutron drip line coincides with the limit of existence of the nucleus, meaning that nuclei beyond the neutron drip line decay. We can see here that the energy needed to separate two- protons from a given isotone is negative such as (⁴⁶Fe to ⁴⁴Cr, ⁴⁷Co to ⁴⁵Mn, ⁴⁸Co to ⁴⁶Mn, ⁴⁸Ni to ⁴⁶Fe, ⁴⁹Ni to ⁴⁷Fe, ⁵²Cu to ⁵⁰Co, ⁵³Cu to ⁵¹Co, ⁵³Zn to ⁵¹Ni, and soon) are negative. Hence, they are not bounded.

And also, as shown in Figure 4.6, when we go from right to left, as proton number decreased, the increment of two-proton separation energy is large amount of factor as isotopes approaches magic nuclei and again it return to the slightly increasing as it goes before. For example the green colored (N=22) curve at ⁵⁰Ni have high separation energy than its neighbor one since it have Z= 28 magic number.

Furthermore, the two-proton separation of double magic nuclei (number magic proton and neutron) is some what greater than that of non-magic nuclei. For instance as shown in the Figure 4.6 cyan colored (N=28) curve, the two-proton separation energy of double magic nuclei ⁵⁶Ni transit to ⁵⁴Fe is higher than S_{2p} of the ⁵⁵Ni transit to ⁵³Fe. The two-protons separation energy from doubly magic nuclei to non-magic nuclei greater than the two-proton separation energy from magic nuclei to non- magic nuclei. Twoproton separation energies exhibit jumps when crossing magic proton numbers. The magnitude of this jump is a measure of the proton magic shell gap for a given neutron number.

In Figure 4.6, The variation in results for the two-protons separation energy also provides important information with regard to the two-proton drip-line. And also the proton number Z is increased for a fixed neutron number N, the S_{2p} decreases until it becomes negative whereby we reach the unbound nucleus or the two-proton drip-line.


Figure 4.6: Two proton separation energy as a function of Z for different N values.



Figure 4.7: Two proton separation energy as a function of N for different Z values.

4.3.2 Two proton separation energy for fixed proton number

This section discussion Figure 4.7 shows that when the number of proton is constant (Z= 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, and 35) the two protons separation energy increases as a function of neutron number, specifically it increases starting from negative to some positive values the way of left to right. This is because of that, the nucleus rich in proton initially below the straight drip line (negative area).

In the Figure 4.7, the result of this work shows that the two-proton separation energy of transitional isotopes increases as the number of neutrons increase with in the nucleus. The Coulomb force of repulsion between the protons becomes large. In order to compensate the large repulsion force there has to be greater number of neutrons. This is due to the contribution of neutrons for stability of the nucleus with in the same nucleus.

Thus two proton separation energy shows discontinuity at different point as neutron number is increases. We can readily understand that in medium heavy nuclei the Coulomb repulsion will favor a neutron-proton distribution with more neutrons than protons.

And also in the Figure 4.7 we can see that the sharp increasing of two-proton separation energy at magic number of either proton or neutron. For instance Scandium-42 having N=20 and Scandium-50 having N=28 the black colored (Z=22) curve have higher two-proton separation energy than the neighbor isotopes. Similarly Nickel-56 the in the middle green colored (Z=28) curve have high two-proton separation energy because of its characteristics of double magic N=28 and Z=28. In addition there is also sharp increasing of two-proton separation energy on three consecutive isotopes of Z=33, 34 and 35, since their neutron is 50 magic number.

4.3.3 Two Neutron Separation Energy for fixed Proton Number

Here the discussion is on Figure 4.8, that we were calculated two-neutron separation energy for fixed proton for varying neutron number. For any fixed number of protons, S_{2n} decreases smoothly as the number of neutron increases. This is because of the symmetry term goes to high for the increasing the difference between the number of proton and the number of neutron, the term is favored for A = 2Z.

For two neutron separation energy, we notice a steady decline in separation energy with increase in neutron number. The evolution of S_{2n} , as a function of neutron number, shows the well-known regularities for any fixed number of protons, S_{2n} decreases smoothly as the number of neutron increases. This decrease mostly has sharp discontinuities at neutron spherical closures magic numbers 20, 28, and 50, i.e. the energy necessary to remove two neutrons from non-magic nuclei is much smaller than that to remove two neutrons from the magic nuclei , and much smaller than is expected from the regular smooth trend. For instance the black colored (Z=20) curve the two neutron separation energy of ⁴⁰Ca is 28 MeV , and at the middle cyan colored (Z=28) for ⁵⁶Ni is 30 MeV, therefore they have high separation energies than neighbor isotopes since they are double magic nuclei. In addition to this on the right of graph green colored (Z=35) curve, ⁸⁵Br have high value of two neutron separation energy than the next Bromine isotopes since it has neutron magic number 50. They indicate very clearly the major shell closures at neutron magic number 50. They indicate very clearly the major shell closures at neutron magic number 50. They indicate of S_{2n} as a function of neutron number.

4.3.4 Two neutron separation energy for fixed neutron number

Under this section Figure 4.9 were plotted as functions of Z while N was kept constant N=19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, and 32. It provides information of Twoneutron separation energies for the neutron-rich nuclei of the isotonic transitions. We can see here two neutron separation energy were calculated for fixed isotone for varying proton number. In Figure 4.9 two neutron separation energy increases as proton number increase for fixed neutron number. If we add more neutrons, they will have to be more energetic, thus increasing the total energy of the nucleus. There fore asymmetry energy term have high effect to make the nucleus have relatively large stability. It can be more easily understood by considering the fact that this term goes to zero for A = 2Z and its effect is smaller for larger A (while for smaller nuclei the symmetry effect is



Figure 4.8: Two neutron separation energy as a function of N for different Z values.



Figure 4.9: Two neutron separation energy as a function of Z for different N values.

more important).

As shown in Figure 4.9 we can get another information, there is sharp increasing of two neutron separation energy observed at ⁵⁰Ti and ⁶⁰Ni, since they have N = 28 and Z = 28, magic number respectively.

4.4 Nucleon Separation Energy and Nuclear Stability in the region 20 \leq Z \leq 35

For stable nuclides having atomic number Z < 20, N=Z or A=2Z, but for Z > 20 the number of neutrons has to be greater than Z for stability of the nucleus. As the result of this work shown that, the behavior of nucleon separation energy depends on different factors. From these factors nucleon number plays a great role. But the effect of proton and neutron with in the nucleus is not the same in all cases. The proton is highly related to the Coulombs effect due to its positive charge. Since Coulombs effect affects the stability of the nucleus, the nucleon separation energy decreases as the proton number is greater than neutron numbers in some nuclei.

In case of considering the magic nuclei, the most of magic nuclei are highly bound and more stable than the nuclei nearby it. Hence, nuclear stability and nucleon separation energy has a relationship. Some times as proton or/and neutron separation energy increases, the stability of the nucleus also increases.

The stability of nuclei is of great interest because unstable nuclei undergo transitions that result in the emission of particles. In the area of this study, we know that in Binding energy per nucleon for Iron (Fe) and Nickel (Ni) has the highest binding energy per nucleon so is the most stable nucleus. Practically, separating nucleons is very essential. For instance removing one proton from ⁵⁷Co and ⁶³Cu will give us ⁵⁶Fe and ⁶²Ni respectively, since ⁵⁶Fe and ⁶²Ni are very stable and having 8.8 MeV Binding energy per nucleon. The energy spend in removing nucleons from a system of identical nucleus shows system stability, which means a nuclei having high separation energy are highly stable and abundant.

Conclusion and Recommendation

In this work, the results of Investigation of One and Two Nucleon Separation Energies for Checking the Nuclear Stability have been performed for isotopes of Atomic number between 20 and 35. From the above analysis we find that the separation energy plays a very important role in understanding the nuclear stability.

Single proton separation energy increases as the neutron number of the given isotope increase for fixed proton. That means additional neutrons requires to assure nuclear stability. A single neutron separation energy not follow the same pattern with one proton separation energy, rather it fluctuate depending on the evenness and oddness of the nucleon numbers of the nuclei as described pairing term. Because of this the maximum (up) peaks have even neutron while minimum (down) peaks have odd neutron number. single proton separation energy along the line of isotones decrease by increasing protons, because asymmetry and Coulomb term reduces the binding energy.

Two proton separation energy decreases as a function of proton number for fixed neutron. Due to increasing of proton number the mass number, A will be large. In case of the increasing of the difference between the number of proton and number of neutron the effect of asymmetry energy term become high then the separation energy decreased. Two-neutron separation energy provides information on the neutron-rich nuclei of the isotonic transitions. Two neutron separation energy increases as proton number increase for fixed neutron number. There fore asymmetry energy term have small value to make the nucleus have relatively large stability.

The one and two nucleon separation energies used to get more fundamental proper-

ties of the atomic nucleus such as isotopic and isotopic transitions. The magic number nuclei are not only highly stable but shows additional characteristics which are greater relative abundances in nature, greater number of stable isotopes, large value of nucleon separation energy and so on. Generally, The energy spend in removing nucleons from a system of identical nucleus shows system stability, which means a nuclei having high separation energy are highly stable and abundant.

We have seen that it is possible to plot and discuss two nucleon separation energies such as two neutron separation energy(S_{2n}) and two proton separation energy(S_{2p}) as a function of either neutron or proton for fixed nucleon number. Which means we have discussed S_{2p} as a function of N for fixed Z and vice versa. And also S_{2n} as a function of Z for fixed N and vice versa. But here we can not have plots and discussion for separation energy of such two nucleon(i.e 1P + 1N) as a function of Z for fixed N, or two nucleon (i.e 1N + 1P) as a function of N for fixed Z. There fore for future the researcher should calculate and check it for further studies.

Calcium	Z	N	A	BE(MeV) [Calc'd]	S _n (MeV)	S_{2n} (MeV)	S _p (MeV)	$S_{2p}(MeV)$
³⁵ Ca	20	15	35	259.45498	-	-	-0.43141	-1.44376
³⁶ Ca	20	16	36	280.61864	21.163660	-	2.3053	1.93469
³⁷ Ca	20	17	37	296.19542	15.576780	36.740440	3.66913	4.76298
³⁸ Ca	20	18	38	314.25827	18.062850	33.639630	4.94777	7.41216
³⁹ Ca	20	19	39	327.68050	12.822230	31.485080	6.84735	10.69944
⁴⁰ Ca	20	20	40	342.50143	15.420930	28.243160	8.46507	14.61545
⁴¹ Ca	20	21	41	352.97427	10.472840	25.293770	10.69958	19.1618
⁴² Ca	20	22	42	366.97427	13.151700	24.472840	14.70445	23.99405
⁴³ Ca	20	23	43	374.57969	8.4537200	21.605420	14.0267	24.95491
⁴⁴ Ca	20	24	44	385.76800	11.188310	18.793730	16.12349	27.21088
⁴⁵ Ca	20	25	45	390.47452	6.7065200	15.894830	14.23235	25.48866
⁴⁶ Ca	20	26	46	401.94276	9.4782400	16.174760	16.26164	27.61237
⁴⁷ Ca	20	27	47	407.13789	5.1951300	16.663370	15.32166	28.77561
⁴⁸ Ca	20	28	48	415.11767	7.9797800	13.174910	15.30622	28.79359
⁴⁹ Ca	20	29	49	418.97051	3.8528400	11.832620	15.30061	29.12961
⁵⁰ Ca	20	30	50	425.62997	6.6594600	10.512300	16.23342	30.7387
⁵¹ Ca	20	31	51	428.31002	2.6800500	9.3395100	14.57546	30.66486
⁵² Ca	20	32	52	433.80021	5.4901900	8.1702400	15.05958	31.47189
⁵³ Ca	20	33	53	435.44290	1.6426900	7.13288	13.95251	32.29536
⁵⁴ Ca	20	34	54	439.89274	4.4498400	6.0925300	15.59098	33.00699
⁵⁵ Ca	20	35	55	440.61384	0.7211000	5.1709400	20.63796	33.73466
⁵⁶ Ca	20	36	56	444.13399	3.5201500	4.2412500	16.43367	_
⁵⁷ Ca	20	37	57	446.03399	1.9000000	5.4201500	16.2387	-
⁵⁸ Ca	20	38	58	446.71904	0.6850500	2.5850500	-	-

Table 5.1: Calculated value of Binding Energy of Isotopes of atomic number between 20 and 35 and their separation energies.

⁵⁹ Ca	20	39	59	446.88191	0.1628700	0.8479200	-	-
⁶⁰ Ca	20	40	60	447.81680	0.9348900	1.0977600	-	-
Scandium								
³⁸ Sc	21	17	38	294.58806	-	-	-1.60736	2.06177
³⁹ Sc	21	18	39	313.94489	19.35683	-	-0.31338	4.63439
⁴⁰ Sc	21	19	40	328.08148	14.13659	33.49342	0.40098	7.24833
⁴¹ Sc	21	20	41	344.73813	16.65665	30.79324	2.2367	10.70177
42 Sc	21	21	42	356.46291	11.72478	28.38143	3.48864	14.18822
⁴³ Sc	21	22	43	370.79142	14.32851	26.05329	3.81715	18.5216
⁴⁴ Sc	21	23	44	380.43534	9.64392	23.97243	5.85565	19.88235
⁴⁵ Sc	21	24	45	392.74247	12.30713	21.95105	6.97447	23.09796
⁴⁶ Sc	21	25	46	400.57924	7.83677	20.1439	10.10472	24.33707
⁴⁷ Sc	21	26	47	411.12021	10.54097	18.37774	9.17745	25.43909
⁴⁸ Sc	21	27	48	417.37817	6.25796	16.79893	10.24028	25.56194
⁴⁹ Sc	21	28	49	426.36703	8.98886	15.24682	11.24936	26.55558
⁵⁰ Sc	21	29	50	431.23811	4.87108	13.85994	12.2676	27.56821
⁵¹ Sc	21	30	51	438.85571	7.6176	12.48868	13.22574	29.45916
⁵² Sc	21	31	52	442.50242	3.64671	11.26431	14.1924	28.76786
⁵³ Sc	21	32	53	448.90262	6.4002	10.04691	15.10241	30.16199
⁵⁴ Sc	21	33	54	451.46342	2.5608	8.961	16.02052	29.97303
⁵⁵ Sc	21	34	55	456.77795	5.31453	7.87533	16.88521	32.47619
⁵⁶ Sc	21	35	56	458.37155	1.5936	6.90813	17.75771	38.39567
⁵⁷ Sc	21	36	57	462.71384	4.34229	5.93589	18.57985	35.01352
⁵⁸ Sc	21	37	58	464.44257	1.72873	6.07102	18.40858	34.64728
⁵⁹ Sc	21	38	59	466.91082	2.46825	4.19698	20.19178	
⁶⁰ Sc	21	39	60	466.86335	-0.04747	2.42078	19.98144	
⁶¹ Sc	21	40	61	469.54301	2.67966	2.63219	21.72621	

Titanium	Z	N	A	BE(MeV) [Calc'd]	S _n (MeV)	S _{2n} (MeV)	S _p (MeV)	$S_{2p}(MeV)$
³⁹ Ti	22	17	39	295.62952	-	-	1.04146	-0.5659
⁴⁰ Ti	22	18	40	316.19380	20.56428	-	2.24891	1.93553
⁴¹ Ti	22	19	41	330.56140	14.3676	34.93188	2.47992	2.8809
⁴² Ti	22	20	42	349.37696	18.81556	33.18316	4.63883	6.87553
⁴³ Ti	22	21	43	362.27968	12.90272	31.71828	5.81677	9.30541
⁴⁴ Ti	22	22	44	377.71671	15.43703	28.33975	6.92529	10.74244
⁴⁵ Ti	22	23	45	388.48497	10.76826	26.20529	8.04963	13.90528
⁴⁶ Ti	22	24	46	400.85011	12.36514	23.1334	8.10764	15.08211
⁴⁷ Ti	22	25	47	410.75841	9.9083	22.27344	10.17917	18.28389
⁴⁸ Ti	22	26	48	420.30702	9.54861	19.45691	9.18681	18.36426
⁴⁹ Ti	22	27	49	429.58610	9.27908	18.82769	12.20793	22.44821
⁵⁰ Ti	22	28	50	439.53543	9.94933	19.22841	13.1684	24.41776
⁵¹ Ti	22	29	51	445.37771	5.84228	15.79161	14.1396	26.4072
⁵² Ti	22	30	52	453.90982	8.53211	14.37439	15.05411	28.27985
⁵³ Ti	22	31	53	458.48091	4.57109	13.1032	15.97849	30.17089
⁵⁴ Ti	22	32	54	465.75188	7.27097	11.84206	16.84926	31.95167
⁵⁵ Ti	22	33	55	469.19268	3.4408	10.71177	17.72926	33.74978
⁵⁶ Ti	22	34	56	475.33651	6.14383	9.58463	18.55856	35.44377
⁵⁷ Ti	22	35	57	477.76818	2.43167	8.5755	19.39663	37.15434
⁵⁸ Ti	22	36	58	482.70059	4.93241	7.36408	19.98675	38.5666
⁵⁹ Ti	22	37	59	484.42786	1.72727	6.65968	19.98529	38.39387
⁶⁰ Ti	22	38	60	488.64929	4.22143	5.9487	21.73847	41.93025
⁶¹ Ti	22	39	61	489.36316	0.71387	4.9353	22.49981	42.48125
⁶² Ti	22	40	62	492.76120	3.39804	4.11191	23.21819	44.9444
⁶³ Ti	22	41	63	492.74109	- 0.02011	3.37793	-	-
⁶⁴ Ti	22	42	64	495.39250	2.65141	2.6313	-	-

Vanadium	Z	N	A	BE(MeV) [Calc'd]	S _n (MeV)	S _{2n} (MeV)	S _p (MeV)	S _{2p} (MeV)
⁴³ V	23	20	43	349.04448	-	-	-0.33248	4.30635
⁴⁴ V	23	21	44	363.13959	14.09511	-	0.85991	6.67668
45 V	23	22	45	379.70202	16.56243	30.65754	1.98531	8.9106
46 V	23	23	46	391.61093	11.90891	28.47134	3.12596	11.17559
⁴⁷ V	23	24	47	406.05250	14.44157	26.35048	5.20239	13.31003
48 V	23	25	48	416.05020	9.9977	24.43927	5.29179	15.47096
49 V	23	26	49	428.62774	12.57754	22.57524	8.32072	17.50753
50 V	23	27	50	436.94548	8.31774	20.89528	7.35938	19.56731
51 V	23	28	51	447.87601	10.93053	19.24827	8.34058	21.50898
52 V	23	29	52	454.70961	6.8336	17.76413	9.3319	23.4715
⁵³ V	23	30	53	464.17777	9.46816	16.30176	10.26795	25.32206
54 V	23	31	54	469.69416	5.51639	14.98455	11.21325	27.19174
⁵⁵ V	23	32	55	477.85801	8.16385	13.68024	12.10613	28.95539
56 V	23	33	56	482.20032	4.34231	12.50616	13.00764	30.7369
57 V	23	34	57	489.19600	6.99568	11.33799	13.85949	32.41805
58 V	23	35	58	492.48768	3.29168	10.28736	14.7195	34.11613
59 V	23	36	59	498.43302	5.94534	9.23702	15.73243	35.71918
⁶⁰ V	23	37	60	500.78106	2.34804	8.29338	16.3532	36.33849
⁶¹ V	23	38	61	505.77864	4.99758	7.34562	17.12935	38.86782
⁶² V	23	39	62	507.27623	1.49759	6.49517	17.91307	40.41288
⁶³ V	23	40	63	511.41569	4.13946	5.63705	18.65449	41.87268
64V	23	41	64	512.14437	0.72868	4.86814	19.40328	-
⁶⁵ V	23	42	65	515.50444	3.36007	4.08875	20.11194	-
⁶⁶ V	23	43	66	515.53585	0.03141	3.39148	-	_
67V	23	44	67	518.18593	2.65008	2.68149	-	-

Chromium	Z	N	Α	BE(MeV) [Calc'd]	S _n (MeV)	S _{2n} (MeV)	S _p (MeV)	S _{2p} (MeV)
⁴¹ Cr	24	17	41	290.38618	-	-	-	-3.24334
⁴² Cr	24	18	42	313.31009	22.92391	-	-	-2.88371
⁴³ Cr	24	19	43	331.08583	17.77574	40.69965	-	0.52443
⁴⁴ Cr	24	20	44	351.17652	20.09069	37.86643	2.13204	1.79956
⁴⁵ Cr	24	21	45	366.39393	15.21741	35.3081	3.25434	4.11425
⁴⁶ Cr	24	22	46	384.01613	17.6222	32.83961	4.31411	6.29942
⁴⁷ Cr	24	23	47	397.00246	12.98633	30.60853	5.39153	8.51749
⁴⁸ Cr	24	24	48	412.46172	15.45926	28.44559	6.40922	11.61161
⁴⁹ Cr	24	25	49	423.49194	11.03022	26.48948	7.44174	12.73353
⁵⁰ Cr	24	26	50	437.04471	13.55277	24.58299	8.41697	16.73769
⁵¹ Cr	24	27	51	446.35062	9.30591	22.85868	9.40514	16.76452
⁵² Cr	24	28	52	458.21460	11.86398	21.16989	10.33859	18.67917
⁵³ Cr	24	29	53	465.99320	7.7786	19.64258	11.28359	20.61549
⁵⁴ Cr	24	30	54	476.35421	10.36101	18.13961	12.17644	22.44439
⁵⁵ Cr	24	31	55	482.77394	6.41973	16.78074	13.07978	24.29303
⁵⁶ Cr	24	32	56	490.79154	8.0176	14.43733	12.93353	25.03966
⁵⁷ Cr	24	33	57	496.99730	6.20576	14.22336	14.79698	27.80462
⁵⁸ Cr	24	34	58	504.80925	7.81195	14.01771	15.61325	29.47274
⁵⁹ Cr	24	35	59	508.92631	4.11706	11.92901	16.43863	31.15813
⁶⁰ Cr	24	36	60	515.65223	6.72592	10.84298	17.21921	32.95164
⁶¹ Cr	24	37	61	518.78947	3.13724	9.86316	18.00841	34.36161
⁶² Cr	24	38	62	524.53366	5.74419	8.88143	18.75502	35.88437
⁶³ Cr	24	39	63	526.78613	2.25247	7.99666	19.5099	37.42297
⁶⁴ Cr	24	40	64	531.64000	4.85387	7.10634	20.22431	38.8788
⁶⁵ Cr	24	41	65	533.09107	1.45107	6.30494	20.9467	40.34998
⁶⁶ Cr	24	42	66	537.13504	4.04397	5.49504	21.6306	41.74254
⁶⁷ Cr	24	43	67	537.85810	0.72306	4.76703	22.32225	-

⁶⁸ Cr	24	44	68	541.16321	3.30511	4.02817	22.97728	-
⁶⁹ Cr	24	45	69	541.22314	0.05993	3.36504	-	-
Manganese								
⁴⁵ Mn	25	20	45	348.55979	-	-	-2.61673	-0.48469
⁴⁶ Mn	25	21	46	364.91128	16.35149	-	-1.48265	1.77169
⁴⁷ Mn	25	22	47	383.60831	18.69703	35.04852	-0.40782	3.90629
⁴⁸ Mn	25	23	48	397.68598	14.07767	32.7747	0.68352	6.07505
⁴⁹ Mn	25	24	49	414.17870	16.49272	30.57039	1.71698	8.1262
⁵⁰ Mn	25	25	50	426.25666	12.07796	28.57068	2.76472	10.20646
⁵¹ Mn	25	26	51	440.80153	14.54487	26.62283	3.75682	12.17379
⁵² Mn	25	27	52	451.11197	10.31044	24.85531	4.76135	14.16649
⁵³ Mn	25	28	53	463.92720	12.81523	23.12567	5.7126	16.05119
⁵⁴ Mn	25	29	54	472.66808	8.74088	21.55611	6.67488	17.95847
⁵⁵ Mn	25	30	55	483.94049	11.27241	20.01329	7.58628	19.76272
⁵⁶ Mn	25	31	56	491.28161	7.34112	18.61353	8.50767	21.58745
⁵⁷ Mn	25	32	57	500.17207	8.89046	16.23158	9.38053	22.31406
⁵⁸ Mn	25	33	58	507.25990	7.08783	15.97829	10.2626	25.05958
⁵⁹ Mn	25	34	59	515.00772	7.74782	14.83565	10.19847	25.81172
⁶⁰ Mn	25	35	60	520.66923	5.66151	13.40933	11.74292	28.18155
⁶¹ Mn	25	36	61	528.39563	7.7264	13.38791	12.7434	29.96261
⁶² Mn	25	37	62	530.34146	1.94583	9.67223	11.55199	29.5604
⁶³ Mn	25	38	63	536.85240	6.51094	8.45677	12.31874	31.07376
⁶⁴ Mn	25	39	64	540.87937	4.02697	10.53791	14.09324	33.60314
⁶⁵ Mn	25	40	65	546.46791	5.58854	9.61551	14.82791	35.05222
⁶⁶ Mn	25	41	66	549.66112	3.19321	8.78175	16.57005	37.51675

⁶⁷ Mn	25	42	67	554.40930	4.74818	7.94139	17.27426	38.90486
⁶⁸ Mn	25	43	68	557.84382	3.43452	8.1827	19.98572	42.30797
⁶⁹ Mn	25	44	69	561.82426	3.98044	7.41496	20.66105	43.63833
⁷⁰ Mn	25	45	70	566.56658	4.74232	8.72276	25.34344	-
⁷¹ Mn	25	46	71	569.84379	3.27721	8.01953	-	-
⁷² Mn	25	47	72	571.95300	2.10921	5.38642	-	-
Iron								
⁴⁵ Ir	26	19	45	327.80050	-	-	-	-3.28533
⁴⁶ Ir	26	20	46	348.95082	21.15032	-	0.39103	-2.2257
⁴⁷ Ir	26	21	47	365.87004	16.91922	38.06954	0.95876	-0.52389
⁴⁸ Ir	26	22	48	385.57938	19.70934	36.62856	1.97107	1.56325
⁴⁹ Ir	26	23	49	400.68801	15.10863	34.81797	3.00203	3.68555
⁵⁰ Ir	26	24	50	418.15779	17.46978	32.57841	3.97909	5.69607
51 Ir	26	25	51	431.22874	13.07095	30.54073	4.97208	7.7368
⁵² Ir	26	26	52	446.71453	15.48579	28.55674	5.913	9.66982
⁵³ Ir	26	27	53	457.97977	11.26524	26.75103	6.8678	11.62915
⁵⁴ Ir	26	28	54	471.69972	13.71995	24.98519	7.77252	13.48512
⁵⁵ Ir	26	29	55	481.35763	9.65791	23.37786	8.68955	15.36443
⁵⁶ Ir	26	30	56	493.09907	11.74144	21.39935	9.15858	16.74486
⁵⁷ Ir	26	31	57	500.72034	7.62127	19.36271	9.43873	17.9464
⁵⁸ Ir	26	32	58	510.44503	9.72469	17.34596	10.27296	19.65349
⁵⁹ Ir	26	33	59	517.37726	6.93223	16.65692	10.11736	20.37996
⁶⁰ Ir	26	34	60	526.82563	9.44837	16.3806	11.81791	22.01638
⁶¹ Ir	26	35	61	530.59713	3.7715	13.21987	9.9279	21.67082
⁶² Ir	26	36	62	539.83166	9.23453	13.00603	11.43603	24.17943
⁶³ Ir	26	37	63	543.61450	3.78284	13.01737	13.27304	24.82503
⁶⁴ Ir	26	38	64	551.86250	8.248	12.03084	15.0101	27.32884
⁶⁵ Ir	26	39	65	556.23497	4.37247	12.62047	15.3556	29.44884
		-	-					

⁶⁶ Ir	26	40	66	563.93088	7.69591	12.06838	17.46297	32.29088
⁶⁷ Ir	26	41	67	567.03953	3.10865	10.80456	17.37841	33.94846
⁶⁸ Ir	26	42	68	573.26679	6.22726	9.33591	18.85749	36.13175
⁶⁹ Ir	26	43	69	575.38816	2.12137	8.34863	17.54434	37.53006
⁷⁰ Ir	26	44	70	580.62074	5.23258	7.35395	18.79648	39.45753
⁷¹ Ir	26	45	71	583.72272	3.10198	8.33456	17.15614	42.49958
⁷² Ir	26	46	72	589.32645	5.60373	8.70571	19.48266	-
⁷³ Ir	26	47	73	591.96950	2.64305	8.24678	20.0165	-
⁷⁴ Ir	26	48	74	589.30316	-2.66634	-0.02329	-	-
⁷⁵ Ir	26	49	75	589.44127	0.13811	-2.52823	-	-
Cobalt								
⁴⁷ Co	27	20	47	347.78765	-	-	-1.16317	-0.77214
⁴⁸ Co	27	21	48	363.28552	15.49787	-	-2.58452	-1.62576
⁴⁹ Co	27	22	49	383.91989	20.63437	36.13224	-1.65949	0.31158
⁵⁰ Co	27	23	50	399.17165	15.25176	35.88613	-1.51636	1.48567
⁵¹ Co	27	24	51	417.63226	18.46061	33.71237	-0.52553	3.45356
⁵² Co	27	25	52	431.70948	14.07722	32.53783	0.48074	5.45282
⁵³ Co	27	26	53	448.15091	16.44143	30.51865	1.43638	7.34938
⁵⁴ Co	27	27	54	460.38518	12.23427	28.6757	2.40541	9.27321
⁵⁵ Co	27	28	55	475.02539	14.64021	26.87448	3.32567	11.09819
⁵⁶ Co	27	29	56	485.61540	10.59001	25.23022	4.25777	12.94732
⁵⁷ Co	27	30	57	498.64208	13.02668	23.61669	5.54301	14.70159
⁵⁸ Co	27	31	58	507.75923	9.11715	22.14383	7.03889	16.47762
⁵⁹ Co	27	32	59	519.33492	11.57569	20.69284	8.88989	19.16285
⁶⁰ Co	27	33	60	527.12786	7.79294	19.36863	9.7506	19.86796
⁶¹ Co	27	34	61	537.39397	10.26611	18.05905	10.56834	22.38625
⁶² Co	27	35	62	543.99223	6.59826	16.86437	13.3951	23.323
⁶³ Co	27	36	63	553.07243	9.0802	15.67846	13.24077	24.6768

⁶⁴ Co	27	37	64	558.58938	5.51695	14.59715	14.97488	28.24792
⁶⁵ Co	27	38	65	566.59224	8.00286	13.51981	14.72974	29.73984
⁶⁶ Co	27	39	66	571.12754	4.5353	12.53816	14.89257	30.24817
⁶⁷ Co	27	40	67	578.14881	7.02127	11.55657	14.21793	31.6809
⁶⁸ Co	27	41	68	581.79043	3.64162	10.66289	14.7509	32.12931
⁶⁹ Co	27	42	69	587.91483	6.1244	9.76602	14.64804	33.50553
⁷⁰ Co	27	43	70	590.74068	2.82585	8.95025	15.35252	32.89686
⁷¹ Co	27	44	71	596.04351	5.30283	8.12868	15.42277	34.21925
⁷² Co	27	45	72	598.12283	2.07932	7.38215	14.40011	31.55625
⁷³ Co	27	46	73	602.67119	4.54836	6.62768	13.34474	32.8274
⁷⁴ Co	27	47	74	604.06575	1.39456	5.94292	12.09625	32.11275
⁷⁵ Co	27	48	75	607.91963	3.85388	5.24844	18.61647	-
⁷⁶ Co	27	49	76	608.68469	0.76506	4.61894	19.24342	-
⁷⁷ Co	27	50	77	611.89793	3.21324	3.9783	-	_
Nickel								
Nickel ⁴⁸ Ni	28	20	48	341.66080	-	-	-3.12685	-5.29002
Nickel ⁴⁸ Ni ⁴⁹ Ni	28 28	20 21	48 49	341.66080 361.17433	- 19.51353	-	-3.12685 -2.11119	-5.29002 -4.69571
Nickel ⁴⁸ Ni ⁴⁹ Ni ⁵⁰ Ni	28 28 28	20 21 22	48 49 50	341.66080 361.17433 382.87468	- 19.51353 21.70035	- - 41.21388	-3.12685 -2.11119 -1.04521	-5.29002 -4.69571 -2.7047
Nickel ⁴⁸ Ni ⁴⁹ Ni ⁵⁰ Ni ⁵¹ Ni	28 28 28 28 28	20 21 22 23	48 49 50 51	341.66080 361.17433 382.87468 400.01209	- 19.51353 21.70035 17.13741	- - 41.21388 38.83776	-3.12685 -2.11119 -1.04521 0.84044	-5.29002 -4.69571 -2.7047 -0.67592
Nickel ⁴⁸ Ni ⁴⁹ Ni ⁵⁰ Ni ⁵¹ Ni ⁵² Ni	28 28 28 28 28 28	20 21 22 23 24	48 49 50 51 52	341.66080 361.17433 382.87468 400.01209 419.40962	- 19.51353 21.70035 17.13741 19.39753	- - 41.21388 38.83776 36.53494	-3.12685 -2.11119 -1.04521 0.84044 1.77736	-5.29002 -4.69571 -2.7047 -0.67592 1.25183
Nickel ⁴⁸ Ni ⁴⁹ Ni ⁵⁰ Ni ⁵¹ Ni ⁵² Ni ⁵³ Ni	28 28 28 28 28 28 28 28	20 21 22 23 24 25	48 49 50 51 52 53	341.66080 361.17433 382.87468 400.01209 419.40962 434.44062	- 19.51353 21.70035 17.13741 19.39753 15.031	- - 41.21388 38.83776 36.53494 34.42853	-3.12685 -2.11119 -1.04521 0.84044 1.77736 2.73114	-5.29002 -4.69571 -2.7047 -0.67592 1.25183 3.21188
${ { Nickel } \\ {}^{48}Ni \\ {}^{49}Ni \\ {}^{50}Ni \\ {}^{51}Ni \\ {}^{52}Ni \\ {}^{53}Ni \\ {}^{54}Ni $	28 28 28 28 28 28 28 28 28	20 21 22 23 24 25 26	48 49 50 51 52 53 54	341.66080 361.17433 382.87468 400.01209 419.40962 434.44062 452.78842	- 19.51353 21.70035 17.13741 19.39753 15.031 18.3478	- - 41.21388 38.83776 36.53494 34.42853 33.3788	-3.12685 -2.11119 -1.04521 0.84044 1.77736 2.73114 4.63751	-5.29002 -4.69571 -2.7047 -0.67592 1.25183 3.21188 6.07389
Nickel ⁴⁸ Ni ⁴⁹ Ni ⁵⁰ Ni ⁵¹ Ni ⁵² Ni ⁵³ Ni ⁵⁴ Ni ⁵⁵ Ni	28 28 28 28 28 28 28 28 28 28	20 21 22 23 24 25 26 27	48 49 50 51 52 53 53 54 55	341.66080 361.17433 382.87468 400.01209 419.40962 434.44062 452.78842 466.94375	- 19.51353 21.70035 17.13741 19.39753 15.031 18.3478 14.15533	- - 41.21388 38.83776 36.53494 34.42853 33.3788 32.50313	-3.12685 -2.11119 -1.04521 0.84044 1.77736 2.73114 4.63751 6.55857	-5.29002 -4.69571 -2.7047 -0.67592 1.25183 3.21188 6.07389 8.96398
Nickel ⁴⁸ Ni ⁴⁹ Ni ⁵⁰ Ni ⁵¹ Ni ⁵² Ni ⁵³ Ni ⁵⁴ Ni ⁵⁵ Ni ⁵⁶ Ni	28 28 28 28 28 28 28 28 28 28 28	20 21 22 23 24 25 26 27 28	48 49 50 51 52 53 54 55 56	341.66080 361.17433 382.87468 400.01209 419.40962 434.44062 452.78842 466.94375 482.45912	- 19.51353 21.70035 17.13741 19.39753 15.031 18.3478 14.15533 15.51537	- 41.21388 38.83776 36.53494 34.42853 33.3788 32.50313 29.6707	-3.12685 -2.11119 -1.04521 0.84044 1.77736 2.73114 4.63751 6.55857 7.43373	-5.29002 -4.69571 -2.7047 -0.67592 1.25183 3.21188 6.07389 8.96398 10.7594
Nickel ⁴⁸ Ni ⁴⁹ Ni ⁵⁰ Ni ⁵¹ Ni ⁵² Ni ⁵³ Ni ⁵⁴ Ni ⁵⁵ Ni ⁵⁶ Ni ⁵⁷ Ni	28 28 28 28 28 28 28 28 28 28 28 28 28	20 21 22 23 24 25 26 27 28 29	48 49 50 51 52 53 54 55 56 57	341.66080 361.17433 382.87468 400.01209 419.40962 434.44062 452.78842 466.94375 482.45912 491.93730	- 19.51353 21.70035 17.13741 19.39753 15.031 18.3478 14.15533 15.51537 9.47818	- 41.21388 38.83776 36.53494 34.42853 33.3788 32.50313 29.6707 24.99355	-3.12685 -2.11119 -1.04521 0.84044 1.77736 2.73114 4.63751 6.55857 7.43373 6.3219	-5.29002 -4.69571 -2.7047 -0.67592 1.25183 3.21188 6.07389 8.96398 10.7594 10.57967
Nickel ⁴⁸ Ni ⁴⁹ Ni ⁵⁰ Ni ⁵¹ Ni ⁵² Ni ⁵³ Ni ⁵⁴ Ni ⁵⁵ Ni ⁵⁶ Ni ⁵⁷ Ni ⁵⁸ Ni	28 28 28 28 28 28 28 28 28 28 28 28 28 2	20 21 22 23 24 25 26 27 28 29 30	48 49 50 51 52 53 53 54 55 56 57 58	341.66080 361.17433 382.87468 400.01209 419.40962 434.44062 452.78842 466.94375 482.45912 491.93730 504.80792	- 19.51353 21.70035 17.13741 19.39753 15.031 18.3478 14.15533 15.51537 9.47818 12.87062	- 41.21388 38.83776 36.53494 34.42853 33.3788 32.50313 29.6707 24.99355 22.3488	-3.12685 -2.11119 -1.04521 0.84044 1.77736 2.73114 4.63751 6.55857 7.43373 6.3219 6.16584	-5.29002 -4.69571 -2.7047 -0.67592 1.25183 3.21188 6.07389 8.96398 10.7594 10.57967 11.70885
Nickel ⁴⁸ Ni ⁴⁹ Ni ⁵⁰ Ni ⁵¹ Ni ⁵² Ni ⁵³ Ni ⁵⁴ Ni ⁵⁵ Ni ⁵⁶ Ni ⁵⁷ Ni ⁵⁸ Ni ⁵⁹ Ni	28 28 28 28 28 28 28 28 28 28 28 28 28 2	20 21 22 23 24 25 26 27 28 29 30 31	48 49 50 51 52 53 54 55 56 57 58 59	341.66080 361.17433 382.87468 400.01209 419.40962 434.44062 452.78842 466.94375 482.45912 491.93730 504.80792 515.78070	- 19.51353 21.70035 17.13741 19.39753 15.031 18.3478 14.15533 15.51537 9.47818 12.87062 10.97278	- 41.21388 38.83776 36.53494 34.42853 33.3788 32.50313 29.6707 24.99355 22.3488 23.8434	-3.12685 -2.11119 -1.04521 0.84044 1.77736 2.73114 4.63751 6.55857 7.43373 6.3219 6.16584 8.02147	-5.29002 -4.69571 -2.7047 -0.67592 1.25183 3.21188 6.07389 8.96398 10.7594 10.57967 11.70885 15.06036

⁶¹ Ni	28	33	61	536.78615	8.61667	21.00545	9.65829	19.40889
⁶² Ni	28	34	62	547.83519	11.04904	19.66571	10.44122	21.00956
⁶³ Ni	28	35	63	555.22618	7.39099	18.44003	11.23395	24.62905
⁶⁴ Ni	28	36	64	565.06	9.83382	17.22481	11.98757	25.22834
⁶⁵ Ni	28	37	65	571.33972	6.27972	16.11354	12.75034	27.72522
⁶⁶ Ni	28	38	66	580.06789	8.72817	15.00789	13.47565	28.20539
⁶⁷ Ni	28	39	67	585.33712	5.26923	13.9974	14.20958	29.10215
⁶⁸ Ni	28	40	68	593.05643	7.71931	12.98854	14.90762	29.12555
⁶⁹ Ni	28	41	69	597.40429	4.34786	12.06717	15.61386	30.36476
⁷⁰ Ni	28	42	70	604.20059	6.7963	11.14416	16.28576	30.9338
⁷¹ Ni	28	43	71	607.70616	3.50557	10.30187	16.96548	32.318
⁷² Ni	28	44	72	613.65584	5.94968	9.45525	17.61233	33.0351
⁷³ Ni	28	45	73	616.38954	2.7337	8.68338	18.26671	32.66682
⁷⁴ Ni	28	46	74	621.56080	5.17126	7.90496	18.88961	32.23435
⁷⁵ Ni	28	47	75	623.58555	2.02475	7.19601	19.5198	31.61605
⁷⁶ Ni	28	48	76	628.03947	4.45392	6.47867	20.11984	38.73631
⁷⁷ Ni	28	49	77	629.41163	1.37216	5.82608	20.72694	39.97036
⁷⁸ Ni	28	50	78	633.20308	3.79145	5.16361	21.30515	-
⁷⁹ Ni	28	51	79	633.97331	0.77023	4.56168	-	-
⁸⁰ Ni	28	52	80	637.15172	3.17841	3.94864	-	-
Copper								
⁵² Cu	29	23	52	396.50215	-	-	-3.50994	-2.6695
⁵³ Cu	29	24	53	416.84891	20.34676	-	-2.56071	-0.78335
⁵⁴ Cu	29	25	54	432.84548	15.99657	36.34333	-1.59514	1.136
⁵⁵ Cu	29	26	55	451.11271	18.26723	34.2638	-1.67571	2.9618
⁵⁶ Cu	29	27	56	465.20170	7 14.08899	32.35622	-1.74205	4.81652
⁵⁷ Cu	29	28	57	481.60601	16.40431	30.4933	-0.85311	6.58062

⁵⁸ Cu	29	29	58	493.98568	12.37967	28.78398	2.04838	8.37028
⁵⁹ Cu	29	30	59	508.71460	14.72892	27.10859	3.90668	10.07252
⁶⁰ Cu	29	31	60	519.55694	10.84234	25.57126	3.77624	11.79771
⁶¹ Cu	29	32	61	532.77367	13.21673	24.05907	4.60419	13.43875
⁶² Cu	29	33	62	542.22853	9.45486	22.67159	5.44238	15.10067
⁶³ Cu	29	34	63	554.07577	11.84724	21.3021	6.24058	16.6818
⁶⁴ Cu	29	35	64	560.72438	6.64861	18.49585	5.4982	16.73215
⁶⁵ Cu	29	36	65	572.87742	12.15304	18.80165	7.81742	19.80499
⁶⁶ Cu	29	37	66	579.03512	6.1577	18.31074	7.6954	20.44574
⁶⁷ Cu	29	38	67	589.40446	10.36934	16.52704	9.33657	22.81222
⁶⁸ Cu	29	39	68	595.42309	6.01863	16.38797	10.08597	24.29555
⁶⁹ Cu	29	40	69	602.85651	7.43342	13.45205	9.80008	24.7077
⁷⁰ Cu	29	41	70	608.92628	6.06977	13.50319	11.52199	27.13585
⁷¹ Cu	29	42	71	616.41067	7.48439	13.55416	12.21008	28.49584
⁷² Cu	29	43	72	620.61177	4.2011	11.68549	12.90561	29.87109
⁷³ Cu	29	44	73	626.22457	5.6128	9.8139	12.56873	30.18106
⁷⁴ Cu	29	45	74	630.62855	4.40398	10.01678	14.23901	32.50572
⁷⁵ Cu	29	46	75	636.43901	5.81046	10.21444	14.87821	33.76782
⁷⁶ Cu	29	47	76	640.19987	3.76086	9.57132	16.61432	36.13412
⁷⁷ Cu	29	48	77	644.18012	3.98025	7.74111	16.14065	36.26049
⁷⁸ Cu	29	49	78	646.17532	1.9952	5.97545	16.76369	37.49063
⁷⁹ Cu	29	50	79	650.56124	4.38592	6.38112	17.35816	38.66331
⁸⁰ Cu	29	51	80	651.93246	1.37122	5.75714	17.95915	-
⁸¹ Cu	29	52	81	655.68446	3.752	5.12322	18.53274	-
⁸² Cu	29	53	82	665.47836	9.7939	13.5459	-	-
Zinc								
⁵⁴ Zn	30	24	54	417.62030	-	-	0.77139	-1.78932
⁵⁵ Zn	30	25	55	433.53228	15.91198	-	0.6868	-0.90834

⁵⁶ Zn	30	26	56	452.67168	19.1394	35.05138	1.55897	-0.11674
⁵⁷ Zn	30	27	57	468.64819	15.97651	35.11591	3.44649	1.70444
⁵⁸ Zn	30	28	58	485.89793	17.24974	33.22625	4.29192	3.43881
⁵⁹ Zn	30	29	59	498.13663	12.2387	29.48844	4.15095	6.19933
⁶⁰ Zn	30	30	60	513.68378	15.54715	27.78585	4.96918	8.87586
⁶¹ Zn	30	31	61	525.35653	11.67275	27.2199	5.79959	9.57583
⁶² Zn	30	32	62	539.36426	14.00773	25.68048	6.59059	11.19478
⁶³ Zn	30	33	63	548.62119	9.25693	23.26466	6.39266	11.83504
⁶⁴ Zn	30	34	64	560.23250	11.61131	20.86824	6.15673	12.39731
⁶⁵ Zn	30	35	65	566.20533	5.97283	17.58414	5.48095	10.97915
⁶⁶ Zn	30	36	66	578.54605	12.34072	18.31355	5.66863	13.48605
⁶⁷ Zn	30	37	67	586.35084	7.80479	20.14551	7.31572	15.01112
⁶⁸ Zn	30	38	68	596.53212	10.18128	17.98607	7.12766	16.46423
⁶⁹ Zn	30	39	69	607.27152	10.7394	20.92068	11.84843	21.9344
⁷⁰ Zn	30	40	70	612.39194	5.12042	15.85982	9.53543	19.33551
⁷¹ Zn	30	41	71	618.15704	5.7651	10.88552	9.23076	20.75275
⁷² Zn	30	42	72	626.30433	8.14729	13.91239	9.89366	22.10374
⁷³ Zn	30	43	73	632.17627	5.87194	14.01923	11.5645	24.47011
⁷⁴ Zn	30	44	74	640.42876	8.25249	14.12443	14.20419	26.77292
⁷⁵ Zn	30	45	75	645.48002	5.05126	13.30375	14.85147	29.09048
⁷⁶ Zn	30	46	76	652.90786	7.42784	12.4791	16.46885	31.34706
⁷⁷ Zn	30	47	77	656.20341	3.29555	10.72339	16.00354	32.61786
⁷⁸ Zn	30	48	78	662.86963	6.66622	9.96177	18.68951	34.83016
⁷⁹ Zn	30	49	79	668.46785	5.59822	12.26444	22.29253	39.05622
⁸⁰ Zn	30	50	80	672.42921	3.96136	9.55958	21.86797	39.22613
⁸¹ Zn	30	51	81	675.38272	2.95351	6.91487	23.45026	41.40941
⁸² Zn	30	52	82	679.69051	4.30779	7.2613	24.00605	42.53879

⁸³ Zn	30	53	83	680.94685	1.25634	5.56413	15.46849	-
⁸⁴ Zn	30	54	84	681.74749	0.80064	2.05698	-	-
⁸⁵ Zn	30	55	85	686.54973	4.80224	5.60288	-	-
⁸⁶ Zn	30	56	86	689.68537	3.13564	7.93788	-	-
Gallium								
⁵⁶ Ga	31	25	56	430.04051	-	-	-3.49177	-2.80497
⁵⁷ Ga	31	26	57	450.06386	20.02335	-	-2.60782	-1.04885
⁵⁸ Ga	31	27	58	466.93925	16.87539	36.89874	-1.70894	1.73755
⁵⁹ Ga	31	28	59	484.04679	17.10754	33.98293	-1.85114	2.44078
⁶⁰ Ga	31	29	60	498.15647	14.10968	31.21722	0.01984	4.17079
⁶¹ Ga	31	30	61	514.53473	16.37826	30.48794	0.85095	5.82013
⁶² Ga	31	31	62	527.95037	12.51564	29.7939	2.59384	8.39343
⁶³ Ga	31	32	63	541.46244	14.81207	26.92771	2.09818	8.68877
⁶⁴ Ga	31	33	64	552.03438	11.07194	24.08401	3.41319	9.80585
⁶⁵ Ga	31	34	65	562.32346	13.38908	20.86102	2.09096	8.24769
⁶⁶ Ga	31	35	66	573.08386	9.760400	21.04948	6.87853	12.35948
⁶⁷ Ga	31	36	67	584.17626	11.0924	21.8528	5.63021	11.29884
⁶⁸ Ga	31	37	68	591.74181	7.56555	18.65795	5.39097	12.70669
⁶⁹ Ga	31	38	69	610.12338	8.47408	18.38157	2.85186	14.70029
⁷⁰ Ga	31	39	70	610.12338	8.47408	18.38157	2.85186	14.70029
⁷¹ Ga	31	40	71	619.64527	9.52189	17.99597	7.25333	16.78876
⁷² Ga	31	41	72	631.99982	12.35455	21.87644	13.84278	23.07354
⁷³ Ga	31	42	73	640.24464	8.24482	20.59937	13.94031	23.83397
⁷⁴ Ga	31	43	74	645.80167	5.55703	13.80185	13.6254	25.1899
⁷⁵ Ga	31	44	75	652.70857	6.9069	12.46393	12.2798	26.484
⁷⁶ Ga	31	45	76	657.42148	4.71291	11.61981	11.94146	26.79293
⁷⁷ Ga	31	46	77	665.48149	8.06001	12.77292	12.57363	29.04248
⁷⁸ Ga	31	47	78	669.41615	3.93466	11.99467	13.21274	29.21628

⁷⁹ Ga	31	48	79	675.69314	6.27699	10.21165	12.82351	31.51302
⁸⁰ Ga	31	49	80	678.90885	3.21571	9.4927	10.441	32.73353
⁸¹ Ga	31	50	81	683.46045	4.5516	7.76731	11.03124	32.89921
⁸² Ga	31	51	82	687.01071	3.55026	8.10186	11.62799	35.07825
⁸³ Ga	31	52	83	691.88904	4.87833	8.42859	12.19853	36.20458
⁸⁴ Ga	31	53	84	692.82226	1.93322	5.81155	11.87541	27.3439
⁸⁵ Ga	31	54	85	701.07458	4.25232	9.18554	19.32709	-
⁸⁶ Ga	31	55	86	702.43466	1.36008	9.6124	15.88493	-
⁸⁷ Ga	31	56	87	704.10390	3.66924	3.02932	14.41853	-
⁸⁸ Ga	31	57	88	705.93075	0.82685	3.49609	-	-
Germanium								
⁵⁸ Ge	32	26	58	449.71505	-	-	-0.34881	-2.95663
⁵⁹ Ge	32	27	59	466.64507	16.93002	-	-0.29418	-2.00312
⁶⁰ Ge	32	28	60	485.96854	19.32347	36.25349	1.92175	0.07061
⁶¹ Ge	32	29	61	500.30826	14.33972	33.66319	2.15179	2.17163
⁶² Ge	32	30	62	517.47887	17.17061	31.51033	2.94414	3.79509
⁶³ Ge	32	31	63	530.79952	13.32065	30.49126	2.84915	5.44299
⁶⁴ Ge	32	32	64	546.38000	15.58048	28.90113	4.91756	7.01574
⁶⁵ Ge	32	33	65	556.23181	9.85181	25.43229	4.19743	7.61062
⁶⁶ Ge	32	34	66	570.06536	13.83355	23.68536	7.7419	9.83286
⁶⁷ Ge	32	35	67	580.88072	10.81536	24.64891	7.79686	14.67539
⁶⁸ Ge	32	36	68	591.99387	11.11315	21.92851	7.81761	13.44782
⁶⁹ Ge	32	37	69	601.98986	9.99599	21.10914	10.24805	15.63902
⁷⁰ Ge	32	38	70	612.59480	10.60494	20.60093	10.9455	16.06268
⁷¹ Ge	32	39	71	620.99537	8.40057	19.00551	10.87199	13.72385
⁷² Ge	32	40	72	631.27195	10.27658	18.67715	11.62668	18.88001
⁷³ Ge	32	41	73	640.42968	9.15773	19.43431	8.42986	22.27264

⁷⁴ Ge	32	42	74	649.90705	9.47737	18.6351	9.66241	23.60272
⁷⁵ Ge	32	43	75	655.12468	5.21763	14.695	9.32301	22.94841
⁷⁶ Ge	32	44	76	661.66269	6.53801	11.75564	8.95412	21.23393
⁷⁷ Ge	32	45	77	667.01436	5.35167	11.88968	9.59288	21.53434
⁷⁸ Ge	32	46	78	678.68474	11.67038	17.02205	13.20325	25.77688
⁷⁹ Ge	32	47	79	683.23712	4.55238	16.22276	13.82097	27.03371
⁸⁰ Ge	32	48	80	691.10449	7.86737	12.41975	15.41135	28.23486
⁸¹ Ge	32	49	81	694.91764	3.81315	11.68052	16.00879	26.44979
⁸² Ge	32	50	82	701.04038	6.12274	9.93589	17.57993	28.61117
⁸³ Ge	32	51	83	704.16859	3.12821	9.25095	17.15788	28.78587
⁸⁴ Ge	32	52	84	710.59954	6.43095	9.55916	18.7105	30.90903
⁸⁵ Ge	32	53	85	713.09199	2.49245	8.9234	20.26973	32.14514
⁸⁶ Ge	32	54	86	717.87915	4.78716	7.27961	16.80457	36.13166
⁸⁷ Ge	32	55	87	719.78049	1.90134	6.6885	17.34583	33.23076
⁸⁸ Ge	32	56	88	723.96749	4.187	6.08834	19.86359	34.28212
⁸⁹ Ge	32	57	89	725.31836	1.35087	5.53787	19.38761	-
⁹⁰ Ge	32	58	90	728.94501	3.62665	4.97752	-	-
Arsenic								
⁶⁰ As	33	27	60	463.92645	-	-	-2.71862	-3.0128
⁶¹ As	33	28	61	482.67713	18.75068	-	-3.29141	-1.36966
⁶² As	33	29	62	498.45775	15.78062	34.5313	-1.85051	0.30128
⁶³ As	33	30	63	516.43242	17.97467	33.75529	-1.04645	1.89769
⁶⁴ As	33	31	64	530.56938	14.13696	32.11163	-0.23014	2.61901
⁶⁵ As	33	32	65	546.93036	16.36098	30.49794	0.55036	5.46792
⁶⁶ As	33	33	66	559.57376	12.6434	29.00438	3.34195	7.53938
⁶⁷ As	33	34	67	572.46421	12.89045	25.53385	2.39885	10.14075
⁶⁸ As	33	35	68	582.74658	10.28237	23.17282	1.86586	9.66272
⁶⁹ As	33	36	69	595.29319	12.54661	22.82898	3.29932	11.11693

⁷⁰ As	33	37	70	604.33199	9.0388	21.58541	2.34213	12.59018
⁷¹ As	33	38	71	616.64732	12.31533	21.35413	4.05252	14.99802
⁷² As	33	39	72	627.54699	10.89967	23.215	6.55162	14.42361
⁷³ As	33	40	73	637.73140	10.18441	21.08408	6.45945	16.08613
⁷⁴ As	33	41	74	643.58512	5.85372	16.03813	5.15544	16.5853
⁷⁵ As	33	42	75	655.72833	12.14321	17.99693	5.82128	15.48369
⁷⁶ As	33	43	76	660.61952	4.89119	17.0344	5.49484	16.81785
⁷⁷ As	33	44	77	670.80203	10.18251	15.0737	9.13934	18.09346
⁷⁸ As	33	45	78	677.00555	6.20352	16.38603	9.99119	19.58407
⁷⁹ As	33	46	79	686.09977	9.09422	15.29774	9.41503	20.61828
⁸⁰ As	33	47	80	693.28302	7.18325	16.27747	10.0459	23.86687
⁸¹ As	33	48	81	701.75429	8.47127	15.65452	10.6498	26.06115
⁸² As	33	49	82	707.17809	5.4238	13.89507	12.26045	28.26924
⁸³ As	33	50	83	713.88549	6.7074	12.1312	12.84511	30.42504
⁸⁴ As	33	51	84	717.60488	3.71939	10.42679	13.43629	30.59417
⁸⁵ As	33	52	85	723.60198	5.9971	9.71649	13.00244	31.71294
⁸⁶ As	33	53	86	726.66689	3.06491	9.06201	13.5749	33.84463
⁸⁷ As	33	54	87	732.00236	5.33547	8.40038	14.12321	30.92778
⁸⁸ As	33	55	88	739.45816	7.4558	12.79127	19.67767	37.0235
⁸⁹ As	33	56	89	742.17635	2.71819	10.17399	18.20886	38.07245
⁹⁰ As	33	57	90	745.06440	2.88805	5.60624	19.74604	39.13365
⁹¹ As	33	58	91	747.20578	2.14138	5.02943	18.26077	-
⁹² As	33	59	92	749.56381	2.35803	4.49941	-	-
Selenium								
⁶³ Se	34	29	63	498.76116	-	-	0.30341	-1.5471
⁶⁴ Se	34	30	64	517.5025	18.74134	-	1.07008	0.02363

⁶⁵ Se	34	31	65	532.41914	14.91664	33.65798	1.84976	1.61962
⁶⁶ Se	34	32	66	548.52584	16.1067	31.02334	1.59548	2.14584
⁶⁷ Se	34	33	67	561.92674	13.4009	29.5076	2.35298	5.69493
⁶⁸ Se	34	34	68	576.54167	14.61493	28.01583	4.07746	6.47631
⁶⁹ Se	34	35	69	587.55930	11.01763	25.63256	4.81272	6.67858
⁷⁰ Se	34	36	70	601.80916	14.24986	25.26749	6.51597	9.81529
⁷¹ Se	34	37	71	612.56114	10.75198	25.00184	8.22915	10.57128
⁷² Se	34	38	72	623.55867	12.99753	21.74951	6.91135	10.96387
⁷³ Se	34	39	73	631.14978	9.591110	18.58864	3.60279	10.15441
⁷⁴ Se	34	40	74	643.99566	11.84588	20.43699	6.26426	12.72371
⁷⁵ Se	34	41	75	651.51953	8.523870	20.36975	7.93441	11.08985
⁷⁶ Se	34	42	76	663.30393	10.78440	19.30827	7.5756	13.39688
⁷⁷ Se	34	43	77	670.84449	7.54056	19.32496	10.22497	15.71981
⁷⁸ Se	34	44	78	680.64842	9.80393	17.34449	9.84639	18.98573
⁷⁹ Se	34	45	79	687.28112	6.6327	16.43663	10.27557	20.26676
⁸⁰ Se	34	46	80	697.17756	8.89644	16.52914	11.07779	18.49282
⁸¹ Se	34	47	81	704.97041	7.79285	17.68929	11.68739	21.73329
⁸² Se	34	48	82	712.02528	8.054870	14.84772	10.27099	20.92079
⁸³ Se	34	49	83	719.03975	5.01447	14.06934	11.86166	24.12211
⁸⁴ Se	34	50	84	728.31274	7.27299	16.28746	14.42725	27.27236
⁸⁵ Se	34	51	85	732.60454	4.2918	13.56479	14.99966	28.43595
⁸⁶ Se	34	52	86	738.14983	5.54529	9.83709	14.54785	27.55029
⁸⁷ Se	34	53	87	742.76951	4.01968	10.16497	16.10262	29.67752
⁸⁸ Se	34	54	88	748.63640	5.06689	10.48657	16.63404	30.75725
⁸⁹ Se	34	55	89	751.63001	2.99361	8.8605	12.17185	31.84952

⁹⁰ Se	34	56	90	756.86345	5.00344	8.22705	14.6871	32.89596
⁹¹ Se	34	57	91	759.27296	2.40951	7.64295	14.20856	33.9546
⁹² Se	34	58	92	763.91403	4.64107	7.05058	16.70825	34.96902
⁹³ Se	34	59	93	765.77780	1.86377	6.50484	16.21399	-
⁹⁴ Se	34	60	94	769.86411	4.08631	5.95008	-	-
⁹⁵ Se	34	61	95	771.21728	1.35317	5.43948	-	-
Bromine								
⁶⁵ Br	35	30	65	514.69812	-	-	-2.80438	-1.7343
⁶⁶ Br	35	31	66	529.40482	15.70670	-	-3.01432	-1.16456
⁶⁷ Br	35	32	67	545.26830	15.86348	30.57018	-3.25754	-1.66206
⁶⁸ Br	35	33	68	560.43741	14.169110	31.03259	-1.48933	0.86365
⁶⁹ Br	35	34	69	576.78819	16.35078	31.51989	0.24652	4.32398
⁷⁰ Br	35	35	70	590.55210	13.76391	30.11469	2.9928	7.80552
⁷¹ Br	35	36	71	603.51682	14.96472	26.72863	1.70766	8.22363
⁷² Br	35	37	72	613.99328	11.476460	23.44118	1.43214	9.66129
⁷³ Br	35	38	73	626.68484	12.69156	23.16802	3.12617	10.03752
⁷⁴ Br	35	39	74	634.97890	10.29406	20.98562	3.82912	7.43191
⁷⁵ Br	35	40	75	648.49827	12.519370	21.81343	4.50261	10.76687
⁷⁶ Br	35	41	76	657.70398	9.20571	22.72508	6.18445	14.11886
⁷⁷ Br	35	42	77	667.14174	9.43776	18.64347	3.83781	11.41341
⁷⁸ Br	35	43	78	676.34351	9.00177	18.63953	5.49902	15.72399
⁷⁹ Br	35	44	79	687.08114	10.73763	19.9394	6.43272	16.27911
⁸⁰ Br	35	45	80	695.05498	7.97384	18.71147	7.77386	18.04943
⁸¹ Br	35	46	81	703.56599	9.51101	16.48485	6.38843	17.46622
⁸² Br	35	47	82	712.90051	6.41452	17.84553	7.9301	19.61749
⁸³ Br	35	48	83	721.63138	8.65087	18.06539	9.6061	19.87709
⁸⁴ Br	35	49	84	729.24866	5.61728	16.34815	10.20891	22.07057

⁸⁵ Br	35	50	85	738.09966	7.85100	16.46828	9.78692	24.21417
⁸⁶ Br	35	51	86	743.07602	4.87636	13.82736	10.47148	25.47114
⁸⁷ Br	35	52	87	749.08194	7.10592	10.98228	10.93211	25.47996
⁸⁸ Br	35	53	88	754.26858	4.18664	11.19256	11.49907	27.60169
⁸⁹ Br	35	54	89	760.67932	6.01074	11.59738	12.04292	28.67696
⁹⁰ Br	35	55	90	764.22289	3.54357	9.95431	12.59288	24.76473
⁹¹ Br	35	56	91	769.08399	4.8611	8.40467	12.22054	26.90764
⁹² Br	35	57	92	772.92709	3.3431	8.7042	13.65413	27.86269
⁹³ Br	35	58	93	777.08021	4.15312	7.99622	13.16618	29.87443
⁹⁴ Br	35	59	94	779.46182	2.38161	6.53473	13.68402	29.89801
⁹⁵ Br	35	60	95	783.04514	3.58332	5.96493	13.18103	-
⁹⁶ Br	35	61	96	785.90096	2.05582	6.43914	14.68368	-
⁹⁷ Br	35	62	97	790.94953	3.04857	7.90439	-	-
⁹⁸ Br	35	63	98	792.31238	1.36285	6.41142	-	-

[Note: All energies are in mega electron-volt(MeV)].

Table 5.2: Transitions of atomic number between 20 and 35 and their neutron separation energies

N	Transition	S _n (MeV)	Transition	S _{2n} (MeV)
18	³⁸ Ca to ³⁷ Ca	18.06285	-	-
18	³⁹ Sc to ³⁸ Sc	19.35683	-	-
18	⁴⁰ Ti to ³⁹ Ti	20.56428	-	-
18	⁴² Cr to ⁴¹ Cr	22.92391	-	-
19	³⁹ Ca to ³⁸ Ca	13.42223	³⁹ Ca to ³⁷ Ca	31.48508
19	⁴⁰ Sc to ³⁹ Sc	14.13659	⁴⁰ Sc to ³⁸ Sc	33.49342
19	⁴¹ Ti to ⁴⁰ Ti	14.3676	⁴¹ Ti to ³⁹ Ti	34.93188
19	⁴³ Cr to ⁴² Cr	17.77574	⁴³ Cr to ⁴¹ Cr	40.69965
20	⁴⁰ Ca to ³⁹ Ca	14.82093	⁴⁰ Ca to ³⁸ Ca	28.24316
20	⁴¹ Sc to ⁴⁰ Sc	16.65665	⁴¹ Sc to ³⁹ Sc	30.79324
20	⁴² Ti to ⁴¹ Ti	18.81556	⁴² Ti to ⁴⁰ Ti	33.18316
20	⁴⁴ Cr to ⁴³ Cr	20.09069	⁴⁴ Cr to ⁴² Cr	37.86643
20	⁴⁶ Fe to ⁴⁵ Fe	21.15032	-	-
21	⁴¹ Ca to ⁴⁰ Ca	10.47284	⁴¹ Ca to ³⁹ Ca	25.29377
21	⁴² Sc to ⁴¹ Sc	11.72478	⁴² Sc to ⁴⁰ Sc	28.38143
21	⁴³ Ti to ⁴² Ti	12.90272	⁴³ Ti to ⁴¹ Ti	31.71828
21	⁴⁴ V to ⁴³ V	14.09511	-	-
21	⁴⁵ Cr to ⁴⁴ Cr	15.21741	⁴⁵ Cr to ⁴³ Cr	35.3081
21	⁴⁶ Mn to ⁴⁵ Mn	16.35149	-	-
21	⁴⁷ Fe to ⁴⁶ Fe	16.91922	⁴⁷ Fe to ⁴⁵ Fe	38.06954
21	⁴⁸ Co to ⁴⁷ Co	15.49787	-	-
21	⁴⁹ Ni to ⁴⁸ Ni	19.51353	-	-

N	Transition	S _n (MeV)	Transition	S_{2n} (MeV)
22	42 Ca to 41 Ca	14	42 Ca to 40 Ca	24.47284
22	43 Sc to 42 Sc	14.32851	⁴³ Sc to ⁴¹ Sc	26.05329
22	⁴⁴ Ti to ⁴³ Ti	15.43703	⁴⁴ Ti to ⁴² Ti	28.33975
22	45 V to 44 V	16.56243	45 V to 43 V	30.65754
22	⁴⁶ Cr to ⁴⁵ Cr	17.6222	⁴⁶ Cr to ⁴⁴ Cr	32.83961
22	47 Mn to 46 Mn	18.69703	47 Mn to 45 Mn	35.04852
22	⁴⁸ Fe to ⁴⁷ Fe	19.70934	⁴⁸ Fe to ⁴⁶ Fe	36.62856
22	⁴⁹ Co to ⁴⁸ Co	20.63437	⁴⁹ Co to ⁴⁷ Co	36.13224
22	⁵⁰ Ni to ⁴⁹ Ni	21.70035	⁵⁰ Ni to ⁴⁸ Ni	41.21388
23	⁴³ Ca to ⁴² Ca	7.60542	⁴³ Ca to ⁴¹ Ca	21.60542
23	⁴⁴ Sc to ⁴³ Sc	9.64392	⁴⁴ Sc to ⁴² Sc	23.97243
23	⁴⁵ Ti to ⁴⁴ Ti	10.76826	⁴⁵ Ti to ⁴³ Ti	26.20529
23	⁴⁶ V to ⁴⁵ V	11.90891	⁴⁶ V to ⁴⁴ V	28.47134
23	⁴⁷ Cr to ⁴⁶ Cr	12.98633	⁴⁷ Cr to ⁴⁵ Cr	30.60853
23	⁴⁸ Mn to ⁴⁷ Mn	14.07767	⁴⁸ Mn to ⁴⁶ Mn	32.7747
23	⁴⁹ Fe to ⁴⁸ Fe	15.10863	⁴⁹ Fe to ⁴⁷ Fe	34.81797
23	⁵⁰ Co to ⁴⁹ Co	15.25176	⁵⁰ Co to ⁴⁸ Co	35.88613
23	⁵¹ Ni to ⁵⁰ Ni	17.13741	⁵¹ Ni to ⁴⁹ Ni	38.83776
24	⁴⁴ Ca to ⁴³ Ca	11.188310	⁴⁴ Ca to ⁴² Ca	18.793730
24	⁴⁵ Sc to ⁴⁴ Sc	12.30713	⁴⁵ Sc to ⁴³ Sc	21.95105
24	⁴⁶ Ti to ⁴⁵ Ti	12.36514	⁴⁶ Ti to ⁴⁴ Ti	23.1334
24	47 V to 46 V	14.44157	47 V to 45 V	26.35048
24	⁴⁸ Cr to ⁴⁷ Cr	15.45926	⁴⁸ Cr to ⁴⁶ Cr	28.44559
24	⁴⁹ Mn to ⁴⁸ Mn	16.49272	⁴⁹ Mn to ⁴⁷ Mn	30.57039

N	Transition	S_n (MeV)	Transition	S_{2n} (MeV)
24	⁵⁰ Fe to ⁴⁹ Fe	17.46978	⁵⁰ Fe to ⁴⁸ Fe	32.57841
24	⁵¹ Co to ⁵⁰ Co	18.46061	⁵¹ Co to ⁴⁹ Co	33.71237
24	⁵² Ni to ⁵¹ Ni	19.39753	⁵² Ni to ⁵⁰ Ni	36.53494
24	⁵³ Cu to ⁵² Cu	20.34676	-	-
25	⁴⁵ Ca to ⁴⁴ Ca	4.7065200	⁴⁵ Ca to ⁴³ Ca	15.894830
25	⁴⁶ Sc to ⁴⁵ Sc	7.83677	⁴⁶ Sc to ⁴⁴ Sc	20.1439
25	⁴⁷ Ti to ⁴⁶ Ti	9.9083	⁴⁷ Ti to ⁴⁵ Ti	22.27344
25	⁴⁸ V to ⁴⁷ V	9.9977	48 V to 46 V	24.43927
25	⁴⁹ Cr to ⁴⁸ Cr	11.03022	⁴⁹ Cr to ⁴⁷ Cr	26.48948
25	⁵⁰ Mn to ⁴⁹ Mn	12.07796	⁵⁰ Mn to ⁴⁸ Mn	28.57068
25	⁵¹ Fe to ⁵⁰ Fe	13.07095	⁵¹ Fe to ⁴⁹ Fe	30.54073
25	⁵² Co to ⁵¹ Co	14.07722	⁵² Co to ⁵⁰ Co	32.53783
25	⁵³ Ni to ⁵² Ni	15.031	⁵³ Ni to ⁵¹ Ni	34.42853
25	⁵⁴ Cu to ⁵³ Cu	15.99657	⁵⁴ Cu to ⁵² Cu	36.34333
25	⁵⁵ Zn to ⁵⁴ Zn	15.91198	-	-
26	46 Ca to 45 Ca	11.468240	⁴⁶ Ca to ⁴⁴ Ca	16.174760
26	⁴⁷ Sc to ⁴⁶ Sc	10.54097	⁴⁷ Sc to ⁴⁵ Sc	18.37774
26	⁴⁸ Ti to ⁴⁷ Ti	9.54861	⁴⁸ Ti to ⁴⁶ Ti	19.45691
26	49 V to 48 V	12.57754	49 V to 47 V	22.57524
26	⁵⁰ Cr to ⁴⁹ Cr	13.55277	⁵⁰ Cr to ⁴⁸ Cr	24.58299
26	51 Mn to 50 Mn	14.54487	51Mn to ⁴⁹ Mn	26.62283
26	⁵² Fe to ⁵¹ Fe	15.48579	⁵² Fe to ⁵⁰ Fe	28.55674
26	⁵³ Co to ⁵² Co	16.44143	⁵³ Co to ⁵¹ Co	30.51865
26	⁵⁴ Ni to ⁵³ Ni	18.3478	⁵⁴ Ni to ⁵² Ni	33.3788
26	⁵⁵ Cu to ⁵⁴ Cu	18.26723	⁵⁵ Cu to ⁵³ Cu	34.2638

N	Transition	S _n (MeV)	Transition	S _{2n} (MeV)
26	⁵⁶ Zn to ⁵⁵ Zn	19.1394	⁵⁶ Zn to ⁵⁴ Zn	35.05138
26	⁵⁷ Ga to ⁵⁶ Ga	20.02335	-	-
27	⁴⁷ Ca to ⁴⁶ Ca	5.1951300	⁴⁷ Ca to ⁴⁵ Ca	16.663370
27	⁴⁸ Sc to ⁴⁷ Sc	6.25796	⁴⁸ Sc to ⁴⁶ Sc	16.79893
27	⁴⁹ Ti to ⁴⁸ Ti	9.27908	⁴⁹ Ti to ⁴⁷ Ti	18.82769
27	$^{50}\mathrm{V}$ to $^{49}\mathrm{V}$	8.31774	$^{50}\mathrm{V}$ to $^{48}\mathrm{V}$	20.89528
27	⁵¹ Cr to ⁵⁰ Cr	9.30591	⁵¹ Cr to ⁴⁹ Cr	22.85868
27	52 Mn to 51 Mn	10.31044	52 Mn to 50 Mn	24.85531
27	⁵³ Fe to ⁵² Fe	11.26524	53Fe to 51Fe	26.75103
27	⁵⁴ Co to ⁵³ Co	12.23427	⁵⁴ Co to ⁵² Co	28.6757
27	⁵⁵ Ni to ⁵⁴ Ni	14.15533	⁵⁵ Ni to ⁵³ Ni	32.50313
27	⁵⁶ Cu to ⁵⁵ Cu	14.08899	⁵⁶ Cu to ⁵⁴ Cu	32.35622
27	⁵⁷ Zn to ⁵⁶ Zn	15.97651	⁵⁷ Zn to ⁵⁵ Zn	35.11591
27	⁵⁸ Ga to ⁵⁷ Ga	16.87539	⁵⁸ Ga to ⁵⁶ Ga	36.89874
27	⁵⁹ Ge to ⁵⁸ Ge	16.93002	-	-
28	⁴⁸ Ca to ⁴⁷ Ca	7.9797800	⁴⁸ Ca to ⁴⁶ Ca	13.174910
28	⁴⁹ Sc to ⁴⁸ Sc	8.98886	⁴⁹ Sc to ⁴⁷ Sc	15.24682
28	⁵⁰ Ti to ⁴⁹ Ti	9.94933	⁵⁰ Ti to ⁴⁸ Ti	19.22841
28	$^{51}\mathrm{V}$ to $^{50}\mathrm{V}$	10.93053	$^{51}\mathrm{V}$ to $^{49}\mathrm{V}$	19.24827
28	⁵² Cr to ⁵¹ Cr	11.86398	⁵² Cr to ⁵⁰ Cr	21.16989
28	53 Mn to 52 Mn	12.81523	⁵³ Mn to ⁵¹ Mn	23.12567
28	⁵⁴ Fe to ⁵³ Fe	13.71995	⁵⁴ Fe to ⁵² Fe	24.98519
28	⁵⁵ Co to ⁵⁴ Co	14.64021	⁵⁵ Co to ⁵³ Co	26.87448
28	⁵⁶ Ni to ⁵⁵ Ni	15.51537	⁵⁶ Ni to ⁵⁴ Ni	29.6707

N	Transition	S _n (MeV)	Transition	S _{2n} (MeV)
28	⁵⁷ Cu to ⁵⁶ Cu	16.40431	⁵⁷ Cu to ⁵⁵ Cu	30.4933
28	⁵⁸ Zn to ⁵⁷ Zn	17.24974	⁵⁸ Zn to ⁵⁶ Zn	33.22625
28	⁵⁹ Ga to ⁵⁸ Ga	17.10754	⁵⁹ Ga to ⁵⁷ Ga	33.98293
28	⁶⁰ Ge to ⁵⁹ Ge	19.32347	-	-
29	⁴⁹ Ca to ⁴⁸ Ca	3.8528400	⁴⁹ Ca to ⁴⁷ Ca	11.832620
29	⁵⁰ Sc to ⁴⁹ Sc	4.87108	⁵⁰ Sc to ⁴⁸ Sc	13.85994
29	⁵¹ Ti to ⁵⁰ Ti	5.84228	⁵¹ Ti to ⁴⁹ Ti	15.79161
29	52 V to 51 V	6.8336	52 V to 50 V	17.76413
29	⁵³ Cr to ⁵² Cr	7.7786	⁵³ Cr to ⁵¹ Cr	19.64258
29	⁵⁴ Mn to ⁵³ Mn	8.74088	⁵⁴ Mn to ⁵² Mn	21.55611
29	⁵⁵ Fe to ⁵⁴ Fe	9.65791	⁵⁵ Fe to ⁵³ Fe	23.37786
29	⁵⁶ Co to ⁵⁵ Co	10.59001	⁵⁶ Co to ⁵⁴ Co	25.23022
29	⁵⁷ Ni to ⁵⁶ Ni	9.47818	⁵⁷ Ni to ⁵⁵ Ni	24.99355
29	⁵⁸ Cu to ⁵⁷ Cu	12.37967	⁵⁸ Cu to ⁵⁶ Cu	28.78398
29	⁵⁹ Zn to ⁵⁸ Zn	12.2387	⁵⁹ Zn to ⁵⁷ Zn	29.48844
29	⁶⁰ Ga to ⁵⁹ Ga	14.10968	⁶⁰ Ga to ⁵⁸ Ga	31.21722
29	⁶¹ Ge to ⁶⁰ Ge	14.33972	⁶¹ Ge to ⁵⁹ Ge	33.66319
29	⁶² As to ⁶¹ As	15.78062	-	-
30	⁵⁰ Ca to ⁴⁹ Ca	6.6594600	⁵⁰ Ca to ⁴⁸ Ca	10.512300
30	51 Sc to 50 Sc	7.6176	51 Sc to 49 Sc	12.48868
30	⁵² Ti to ⁵¹ Ti	8.53211	⁵² Ti to ⁵⁰ Ti	14.37439
30	53 V to 52 V	9.46816	53 V to 51 V	16.30176
30	⁵⁴ Cr to ⁵³ Cr	10.36101	⁵⁴ Cr to ⁵² Cr	18.13961
30	⁵⁵ Mn to ⁵⁴ Mn	11.27241	⁵⁵ Mn to ⁵³ Mn	20.01329
30	⁵⁶ Fe to ⁵⁵ Fe	11.74144	⁵⁶ Fe to ⁵⁴ Fe	21.39935

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N	Transition	S _n (MeV)	Transition	S_{2n} (MeV)
30	⁵⁷ Co to ⁵⁶ Co	13.02668	⁵⁷ Co to ⁵⁵ Co	23.61669
30	⁵⁸ Ni to ⁵⁷ Ni	12.87062	⁵⁸ Ni to ⁵⁶ Ni	22.3488
30	⁵⁹ Cu to ⁵⁸ Cu	14.72892	⁵⁹ Cu to ⁵⁷ Cu	27.10859
30	⁶⁰ Zn to ⁵⁹ Zn	15.54715	⁶⁰ Zn to ⁵⁸ Zn	27.78585
30	⁶¹ Ga to ⁶⁰ Ga	16.37826	⁶¹ Ga to ⁵⁹ Ga	30.48794
30	⁶² Ge to ⁶¹ Ge	17.17061	⁶² Ge to ⁶⁰ Ge	31.51033
30	⁶³ As to ⁶² As	17.97467	⁶³ As to ⁶¹ As	33.75529
30	⁶⁴ Se to ⁶³ Se	18.74134	-	-
31	⁵¹ Ca to ⁵⁰ Ca	2.6800500	⁵¹ Ca to ⁴⁹ Ca	9.3395100
31	⁵² Sc to ⁵¹ Sc	3.64671	⁵² Sc to ⁵⁰ Sc	11.26431
31	⁵³ Ti to ⁵² Ti	4.57109	⁵³ Ti to ⁵¹ Ti	13.1032
31	54 V to 53 V	5.51639	54 V to 52 V	14.98455
31	⁵⁵ Cr to ⁵⁴ Cr	6.41973	⁵⁵ Cr to ⁵³ Cr	16.78074
31	⁵⁶ Mn to ⁵⁵ Mn	7.34112	⁵⁶ Mn to ⁵⁴ Mn	18.61353
31	⁵⁷ Fe to ⁵⁶ Fe	7.62127	⁵⁷ Fe to ⁵⁵ Fe	19.36271
31	⁵⁸ Co to ⁵⁷ Co	9.11715	⁵⁸ Co to ⁵⁶ Co	22.14383
31	⁵⁹ Ni to ⁵⁸ Ni	10.97278	⁵⁹ Ni to ⁵⁷ Ni	23.8434
31	⁶⁰ Cu to ⁵⁹ Cu	10.84234	⁶⁰ Cu to ⁵⁸ Cu	25.57126
31	⁶¹ Zn to ⁶⁰ Zn	11.67275	⁶¹ Zn to ⁵⁹ Zn	27.2199
31	⁶² Ga to ⁶¹ Ga	13.41564	⁶² Ga to ⁶⁰ Ga	29.7939
31	⁶³ Ge to ⁶² Ge	13.32065	⁶³ Ge to ⁶¹ Ge	30.49126
31	⁶⁴ As to ⁶³ As	14.13696	⁶⁴ As to ⁶² As	32.11163
31	⁶⁵ Se to ⁶⁴ Se	14.91664	⁶⁵ Se to ⁶³ Se	33.65798
31	⁶⁶ Br to ⁶⁵ Br	14.7067	-	-

N	Transition	S _n (MeV)	Transition	S _{2n} (MeV)
32	⁵² Ca to ⁵¹ Ca	5.4901900	⁵² Ca to ⁵⁰ Ca	8.1702400
32	⁵³ Sc to ⁵² Sc	6.4002	⁵³ Sc to ⁵¹ Sc	10.04691
32	⁵⁴ Ti to ⁵³ Ti	7.27097	⁵⁴ Ti to ⁵² Ti	11.84206
32	55 V to 54 V	8.16385	55 V to 53 V	13.68024
32	⁵⁶ Cr to ⁵⁵ Cr	8.0176	⁵⁶ Cr to ⁵⁴ Cr	14.43733
32	⁵⁷ Mn to ⁵⁶ Mn	8.89046	⁵⁷ Mn to ⁵⁵ Mn	16.23158
32	⁵⁸ Fe to ⁵⁷ Fe	9.72469	⁵⁸ Fe to ⁵⁶ Fe	17.34596
32	⁵⁹ Co to ⁵⁸ Co	11.57569	⁵⁹ Co to ⁵⁷ Co	20.69284
32	⁶⁰ Ni to ⁵⁹ Ni	12.38878	⁶⁰ Ni to ⁵⁸ Ni	23.36156
32	⁶¹ Cu to ⁶⁰ Cu	13.21673	⁶¹ Cu to ⁵⁹ Cu	24.05907
32	⁶² Zn to ⁶¹ Zn	14.00773	⁶² Zn to ⁶⁰ Zn	25.68048
32	⁶³ Ga to ⁶² Ga	13.51207	⁶³ Ga to ⁶¹ Ga	26.92771
32	⁶⁴ Ge to ⁶³ Ge	15.58048	⁶⁴ Ge to ⁶² Ge	28.90113
32	⁶⁵ As to ⁶⁴ As	16.36098	⁶⁵ As to ⁶³ As	30.49794
32	⁶⁶ Se to ⁶⁵ Se	16.1067	66Se to 64Se	31.02334
32	⁶⁷ Br to ⁶⁶ Br	15.86348	⁶⁷ Br to ⁶⁵ Br	30.57018

Table 5.3:	Isotonic transitions of atomic number between 20 and 35 and their proton
separation	energies

N	Isotonic Transition	$S_p(MeV)$	Isotonic Transition	$S_{2p}(MeV)$
20	⁴¹ Sc to ⁴⁰ Ca	2.2367	-	-
20	⁴² Ti to ⁴¹ Sc	4.63883	⁴² Ti to ⁴⁰ Ca	6.87553
20	⁴³ V to ⁴² Ti	-0.33248	43 V to 41 Sc	4.30635
20	⁴⁴ Cr to ⁴³ V	2.13204	⁴⁴ Cr to ⁴² Ti	1.79956
20	⁴⁵ Mn to ⁴⁴ Cr	-2.61673	45 Mn to 43 V	-0.48469
20	⁴⁶ Fe to ⁴⁵ Mn	0.39103	⁴⁶ Fe to ⁴⁴ Cr	-2.2257
20	⁴⁷ Co to ⁴⁶ Fe	-1.16317	⁴⁷ Co to ⁴⁵ Mn	-0.77214
20	⁴⁸ Ni to ⁴⁷ Co	-6.12685	⁴⁸ Ni to ⁴⁶ Fe	-7.29002
21	⁴² Sc to ⁴¹ Ca	3.48864	-	-
21	⁴³ Ti to ⁴² Sc	5.81677	⁴³ Ti to ⁴¹ Ca	9.30541
21	⁴⁴ V to ⁴³ Ti	0.85991	⁴⁴ V to ⁴² Sc	6.67668
21	⁴⁵ Cr to ⁴⁴ V	3.25434	⁴⁵ Cr to ⁴³ Ti	4.11425
21	⁴⁶ Mn to ⁴⁵ Cr	-1.48265	⁴⁶ Mn to 44V	1.77169
21	⁴⁷ Fe to ⁴⁶ Mn	0.95876	⁴⁷ Fe to ⁴⁵ Cr	-0.52389
21	⁴⁸ Co to ⁴⁷ Fe	-2.58452	⁴⁸ Co to ⁴⁶ Mn	-1.62576
21	⁴⁹ Ni to ⁴⁸ Co	-2.11119	⁴⁹ Ni to ⁴⁷ Fe	-4.69571
22	⁴³ Sc to ⁴² Ca	3.81715	-	-
22	⁴⁴ Ti to ⁴³ Sc	6.92529	⁴⁴ Ti to ⁴² Ca	10.74244
22	⁴⁵ V to ⁴⁴ Ti	1.98531	45 V to 43 Sc	8.9106
22	⁴⁶ Cr to ⁴⁵ V	4.31411	⁴⁶ Cr to ⁴⁴ Ti	6.29942
22	⁴⁷ Mn to ⁴⁶ Cr	-0.40782	⁴⁷ Mn to ⁴⁵ V	3.90629
22	⁴⁸ Fe to ⁴⁷ Mn	1.97107	⁴⁸ Fe to ⁴⁶ Cr	1.56325
22	⁴⁹ Co to ⁴⁸ Fe	-1.65949	⁴⁹ Co to ⁴⁷ Mn	0.31158

N	Isotonic Transition	S _p (MeV)	Isotonic Transition	$S_{2p}(MeV)$
22	⁵⁰ Ni to 49Co	-1.04521	50Ni to 48Fe	-2.7047
23	⁴⁴ Sc to ⁴³ Ca	5.85565	-	-
23	⁴⁵ Ti to ⁴⁴ Sc	8.04963	⁴⁵ Ti to ⁴³ Ca	13.90528
23	⁴⁶ V to ⁴⁵ Ti	3.12596	⁴⁶ V to ⁴⁴ Sc	11.17559
23	⁴⁷ Cr to ⁴⁶ V	5.39153	⁴⁷ Cr to ⁴⁵ Ti	8.51749
23	⁴⁸ Mn to ⁴⁷ Cr	0.68352	48 Mn to 46 V	6.07505
23	⁴⁹ Fe to 48Mn	3.00203	49Fe to 47Cr	3.68555
23	⁵⁰ Co to ⁴⁹ Fe	-1.51636	⁵⁰ Co to ⁴⁸ Mn	1.48567
23	⁵¹ Ni to ⁵⁰ Co	0.84044	⁵¹ Ni to ⁴⁹ Fe	-0.67592
23	⁵² Cu to ⁵¹ Ni	-3.50994	⁵² Cu to ⁵⁰ Co	-2.6695
24	⁴⁵ Sc to ⁴⁴ Ca	6.97447	-	-
24	⁴⁶ Ti to ⁴⁵ Sc	8.10764	⁴⁶ Ti to ⁴⁴ Ca	15.08211
24	⁴⁷ V to ⁴⁶ Ti	5.20239	47 V to 45 Sc	13.31003
24	⁴⁸ Cr to ⁴⁷ V	6.40922	⁴⁸ Cr to ⁴⁶ Ti	11.61161
24	⁴⁹ Mn to ⁴⁸ Cr	1.71698	⁴⁹ Mn to ⁴⁷ V	8.1262
24	⁵⁰ Fe to ⁴⁹ Mn	3.97909	⁵⁰ Fe to ⁴⁸ Cr	5.69607
24	⁵¹ Co to ⁵⁰ Fe	-0.52553	⁵¹ Co to ⁴⁹ Mn	3.45356
24	⁵² Ni to ⁵¹ Co	1.77736	⁵² Ni to ⁵⁰ Fe	1.25183
24	⁵³ Cu to ⁵² Ni	-2.56071	⁵³ Cu to ⁵¹ Co	-0.78335
24	⁵⁴ Zn to ⁵³ Cu	0.77139	⁵⁴ Zn to ⁵² Ni	-1.78932
25	⁴⁶ Sc to ⁴⁵ Ca	10.10472	-	-
25	⁴⁷ Ti to ⁴⁶ Sc	10.17917	47 Ti to 45 Ca	20.28389
25	⁴⁸ V to ⁴⁷ Ti	5.29179	⁴⁸ V to ⁴⁶ Sc	15.47096
25	⁴⁹ Cr to ⁴⁸ V	7.44174	⁴⁹ Cr to ⁴⁷ Ti	12.73353
25	⁵⁰ Mn to ⁴⁹ Cr	2.76472	50 Mn to 48 V	10.20646

N	Isotonic Transition	S _p (MeV)	Isotonic Transition	$S_{2p}(MeV)$
25	⁵¹ Fe to ⁵⁰ Mn	4.97208	⁵¹ Fe to 49Cr	7.7368
25	⁵² Co to ⁵¹ Fe	0.48074	⁵² Co to ⁵⁰ Mn	5.45282
25	⁵³ Ni to ⁵² Co	2.73114	⁵³ Ni to ⁵¹ Fe	3.21188
25	⁵⁴ Cu to ⁵³ Ni	-1.59514	⁵⁴ Cu to ⁵² Co	1.136
25	⁵⁵ Zn to ⁵⁴ Cu	0.6868	⁵⁵ Zn to ⁵³ Ni	-0.90834
25	⁵⁶ Ga to ⁵⁵ Zn	-3.49177	⁵⁶ Ga to ⁵⁴ Cu	-2.80497
26	⁴⁷ Sc to ⁴⁶ Ca	9.17745	-	-
26	⁴⁸ Ti to ⁴⁷ Sc	9.18681	⁴⁸ Ti to ⁴⁶ Ca	18.36426
26	⁴⁹ V to ⁴⁸ Ti	8.32072	49 V to 47 Sc	17.50753
26	⁵⁰ Cr to ⁴⁹ V	8.41697	⁵⁰ Cr to ⁴⁸ Ti	16.73769
26	$^{51}{ m Mn}$ to $^{50}{ m Cr}$	3.75682	$^{51}\mathrm{Mn}$ to $^{49}\mathrm{V}$	12.17379
26	⁵² Fe to ⁵¹ Mn	5.913	⁵² Fe to ⁵⁰ Cr	9.66982
26	⁵³ Co to ⁵² Fe	1.43638	⁵³ Co to ⁵¹ Mn	7.34938
26	⁵⁴ Ni to ⁵³ Co	4.63751	⁵⁴ Ni to ⁵² Fe	6.07389
26	⁵⁵ Cu to ⁵⁴ Ni	-1.67571	⁵⁵ Cu to ⁵³ Co	2.9618
26	⁵⁶ Zn to ⁵⁵ Cu	1.55897	⁵⁶ Zn to ⁵⁴ Ni	-0.11674
26	⁵⁷ Ga to ⁵⁶ Zn	-2.60782	⁵⁷ Ga to ⁵⁵ Cu	-1.04885
26	⁵⁸ Ge to ⁵⁷ Ga	-0.34881	⁵⁸ Ge to ⁵⁶ Zn	-2.95663
27	⁴⁸ Sc to ⁴⁷ Ca	10.24028	-	-
27	⁴⁹ Ti to ⁴⁸ Sc	12.20793	⁴⁹ Ti to ⁴⁷ Ca	22.44821
27	⁵⁰ V to ⁴⁹ Ti	7.35938	50 V to 48 Sc	19.56731
27	⁵¹ Cr to ⁵⁰ V	9.40514	⁵¹ Cr to ⁴⁹ Ti	16.76452
27	⁵² Mn to ⁵¹ Cr	4.76135	52 Mn to 50 V	14.16649
27	⁵³ Fe to ⁵² Mn	6.8678	⁵³ Fe to ⁵¹ Cr	11.62915
27	⁵⁴ Co to ⁵³ Fe	2.40541	⁵⁴ Co to ⁵² Mn	9.27321
27	⁵⁵ Ni to ⁵⁴ Co	6.55857	⁵⁵ Ni to ⁵³ Fe	8.96398
N	Isotonic Transition	$S_p(MeV)$	Isotonic Transition	$S_{2p}(MeV)$
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27	⁵⁶ Cu to ⁵⁵ Ni	-1.74205	⁵⁶ Cu to ⁵⁴ Co	4.81652
27	⁵⁷ Zn to ⁵⁶ Cu	3.44649	⁵⁷ Zn to ⁵⁵ Ni	1.70444
27	⁵⁸ Ga to ⁵⁷ Zn	-1.70894	⁵⁸ Ga to ⁵⁶ Cu	1.73755
27	⁵⁹ Ge to ⁵⁸ Ga	-0.29418	⁵⁹ Ge to ⁵⁷ Zn	-2.00312
27	⁶⁰ As to ⁵⁹ Ge	-2.71862	⁶⁰ As to ⁵⁸ Ga	-3.0128
28	⁴⁹ Sc to ⁴⁸ Ca	11.24936	-	-
28	⁵⁰ Ti to ⁴⁹ Sc	13.1684	⁵⁰ Ti to ⁴⁸ Ca	24.41776
28	⁵¹ V to ⁵⁰ Ti	8.34058	$^{51}\mathrm{V}\mathrm{to}{}^{49}\mathrm{Sc}$	21.50898
28	⁵² Cr to ⁵¹ V	10.33859	⁵² Cr to ⁵⁰ Ti	18.67917
28	⁵³ Mn to ⁵² Cr	5.7126	$^{53}\mathrm{Mn}$ to $^{51}\mathrm{V}$	16.05119
28	⁵⁴ Fe to ⁵³ Mn	7.77252	⁵⁴ Fe to ⁵² Cr	13.48512
28	⁵⁵ Co to ⁵⁴ Fe	3.32567	⁵⁵ Co to ⁵³ Mn	11.09819
28	⁵⁶ Ni to ⁵⁵ Co	6.91191	⁵⁶ Ni to ⁵⁴ Fe	12.23758
28	⁵⁷ Cu to ⁵⁶ Ni	-0.33129	⁵⁷ Cu to ⁵⁵ Co	6.58062
28	⁵⁸ Zn to ⁵⁷ Cu	4.29192	⁵⁸ Zn to ⁵⁶ Ni	6.03937
28	⁵⁹ Ga to ⁵⁸ Zn	-1.85114	⁵⁹ Ga to ⁵⁷ Cu	2.44078
28	⁶⁰ Ge to ⁵⁹ Ga	1.92175	⁶⁰ Ge to ⁵⁸ Zn	0.07061
28	⁶¹ As to ⁶⁰ Ge	-3.29141	⁶¹ As to ⁵⁹ Ga	-1.36966
29	⁵⁰ Sc to ⁴⁹ Ca	12.2676	-	-
29	⁵¹ Ti to ⁵⁰ Sc	14.1396	⁵¹ Ti to ⁴⁹ Ca	26.4072
29	⁵² V to ⁵¹ Ti	9.3319	52 V to 50 Sc	23.4715
29	⁵³ Cr to ⁵² V	11.28359	⁵³ Cr to ⁵¹ Ti	20.61549
29	⁵⁴ Mn to ⁵³ Cr	6.67488	$^{54}\mathrm{Mn}$ to $^{52}\mathrm{V}$	17.95847
29	⁵⁵ Fe to ⁵⁴ Mn	8.68955	⁵⁵ Fe to ⁵³ Cr	15.36443
29	⁵⁶ Co to ⁵⁵ Fe	4.25777	⁵⁶ Co to ⁵⁴ Mn	12.94732

N	Isotonic Transition	S _p (MeV)	Isotonic Transition	$S_{2p}(MeV)$
29	⁵⁷ Ni to ⁵⁶ Co	6.3219	⁵⁷ Ni to ⁵⁵ Fe	10.57967
29	⁵⁸ Cu to ⁵⁷ Ni	2.04838	⁵⁸ Cu to ⁵⁶ Co	8.37028
29	⁵⁹ Zn to ⁵⁸ Cu	4.15095	⁵⁹ Zn to ⁵⁷ Ni	6.19933
29	⁶⁰ Ga to ⁵⁹ Zn	0.01984	⁶⁰ Ga to ⁵⁸ Cu	4.17079
29	⁶¹ Ge to ⁶⁰ Ga	2.15179	⁶¹ Ge to ⁵⁹ Zn	2.17163
29	⁶² As to ⁶¹ Ge	-1.85051	⁶² As to ⁶⁰ Ga	0.30128
29	⁶³ Se to ⁶² As	0.30341	⁶³ Se to ⁶¹ Ge	-1.5471
30	⁵¹ Sc to ⁵⁰ Ca	13.22574	-	-
30	⁵² Ti to ⁵¹ Sc	15.05411	⁵² Ti to ⁵⁰ Ca	28.27985
30	⁵³ V to ⁵² Ti	10.26795	⁵³ V to ⁵¹ Sc	25.32206
30	⁵⁴ Cr to ⁵³ V	12.17644	⁵⁴ Cr to ⁵² Ti	22.44439
30	⁵⁵ Mn to ⁵⁴ Cr	7.58628	$^{55}\mathrm{Mn}$ to $^{53}\mathrm{V}$	19.76272
30	⁵⁶ Fe to ⁵⁵ Mn	9.15858	⁵⁶ Fe to ⁵⁴ Cr	16.74486
30	⁵⁷ Co to ⁵⁶ Fe	5.54301	⁵⁷ Co to ⁵⁵ Mn	14.70159
30	⁵⁸ Ni to ⁵⁷ Co	6.16584	⁵⁸ Ni to ⁵⁶ Fe	11.70885
30	⁵⁹ Cu to ⁵⁸ Ni	3.90668	⁵⁹ Cu to ⁵⁷ Co	10.07252
30	⁶⁰ Zn to ⁵⁹ Cu	4.96918	⁶⁰ Zn to ⁵⁸ Ni	8.87586
30	⁶¹ Ga to ⁶⁰ Zn	0.85095	⁶¹ Ga to ⁵⁹ Cu	5.82013
30	⁶² Ge to ⁶¹ Ga	2.94414	⁶² Ge to ⁶⁰ Zn	3.79509
30	⁶³ As to ⁶² Ge	-1.04645	⁶³ As to ⁶¹ Ga	1.89769
30	⁶⁴ Se to ⁶³ As	1.07008	⁶⁴ Se to ⁶² Ge	0.02363
30	⁶⁵ Br to ⁶⁴ Se	-2.80438	⁶⁵ Br to ⁶³ As	-1.7343
31	⁵² Sc to ⁵¹ Ca	14.1924	-	-
31	⁵³ Ti to ⁵² Sc	15.97849	⁵³ Ti to ⁵¹ Ca	30.17089
31	⁵⁴ V to ⁵³ Ti	11.21325	⁵⁴ V to ⁵² Sc	27.19174
31	⁵⁵ Cr to ⁵⁴ V	13.07978	⁵⁵ Cr to ⁵³ Ti	24.29303

N	Isotonic Transition	S _p (MeV)	Isotonic Transition	$S_{2p}(MeV)$
31	$^{56}\mathrm{Mn}$ to $^{55}\mathrm{Cr}$	8.50767	$^{56}\mathrm{Mn}$ to $^{54}\mathrm{V}$	21.58745
31	⁵⁷ Fe to ⁵⁶ Mn	9.43873	⁵⁷ Fe to ⁵⁵ Cr	17.9464
31	⁵⁸ Co to ⁵⁷ Fe	7.03889	⁵⁸ Co to ⁵⁶ Mn	16.47762
31	⁵⁹ Ni to ⁵⁸ Co	8.02147	⁵⁹ Ni to ⁵⁷ Fe	15.06036
31	⁶⁰ Cu to ⁵⁹ Ni	3.77624	⁶⁰ Cu to ⁵⁸ Co	11.79771
31	⁶¹ Zn to ⁶⁰ Cu	5.79959	⁶¹ Zn to ⁵⁹ Ni	9.57583
31	⁶² Ga to ⁶¹ Zn	2.59384	⁶² Ga to ⁶⁰ Cu	8.39343
31	⁶³ Ge to ⁶² Ga	2.84915	⁶³ Ge to ⁶¹ Zn	5.44299
31	⁶⁴ As to ⁶³ Ge	-0.23014	⁶⁴ As to ⁶² Ga	2.61901
31	⁶⁵ Se to ⁶⁴ As	1.84976	⁶⁵ Se to ⁶³ Ge	1.61962
31	⁶⁶ Br to ⁶⁵ Se	-3.01432	⁶⁶ Br to ⁶⁴ As	-1.16456
32	⁵³ Sc to ⁵² Ca	15.10241	-	-
32	⁵⁴ Ti to ⁵³ Sc	16.84926	⁵⁴ Ti to ⁵² Ca	31.95167
32	55 V to 54 Ti	12.10613	$^{55}\mathrm{V}$ to $^{53}\mathrm{Sc}$	28.95539
32	⁵⁶ Cr to ⁵⁵ V	12.93353	⁵⁶ Cr to ⁵⁴ Ti	25.03966
32	$^{57}\mathrm{Mn}$ to $^{56}\mathrm{Cr}$	9.38053	$^{57}\mathrm{Mn}$ to $^{55}\mathrm{V}$	22.31406
32	⁵⁸ Fe to ⁵⁷ Mn	10.27296	⁵⁸ Fe to ⁵⁶ Cr	19.65349
32	⁵⁹ Co to ⁵⁸ Fe	8.88989	⁵⁹ Co to ⁵⁷ Mn	19.16285
32	⁶⁰ Ni to ⁵⁹ Co	8.83456	⁶⁰ Ni to ⁵⁸ Fe	17.72445
32	⁶¹ Cu to ⁶⁰ Ni	4.60419	⁶¹ Cu to ⁵⁹ Co	13.43875
32	⁶² Zn to ⁶¹ Cu	6.59059	⁶² Zn to ⁶⁰ Ni	11.19478
32	⁶³ Ga to ⁶² Zn	2.09818	⁶³ Ga to ⁶¹ Cu	8.68877
32	⁶⁴ Ge to ⁶³ Ga	4.91756	⁶⁴ Ge to ⁶² Zn	7.01574
32	⁶⁵ As to ⁶⁴ Ge	0.55036	⁶⁵ As to ⁶³ Ga	5.46792
32	⁶⁶ Se to ⁶⁵ As	1.59548	⁶⁶ Se to ⁶⁴ Ge	-3.96086
32	⁶⁷ Br to ⁶⁶ Se	-3.25754	⁶⁷ Br to ⁶⁵ As	-1.66206

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